

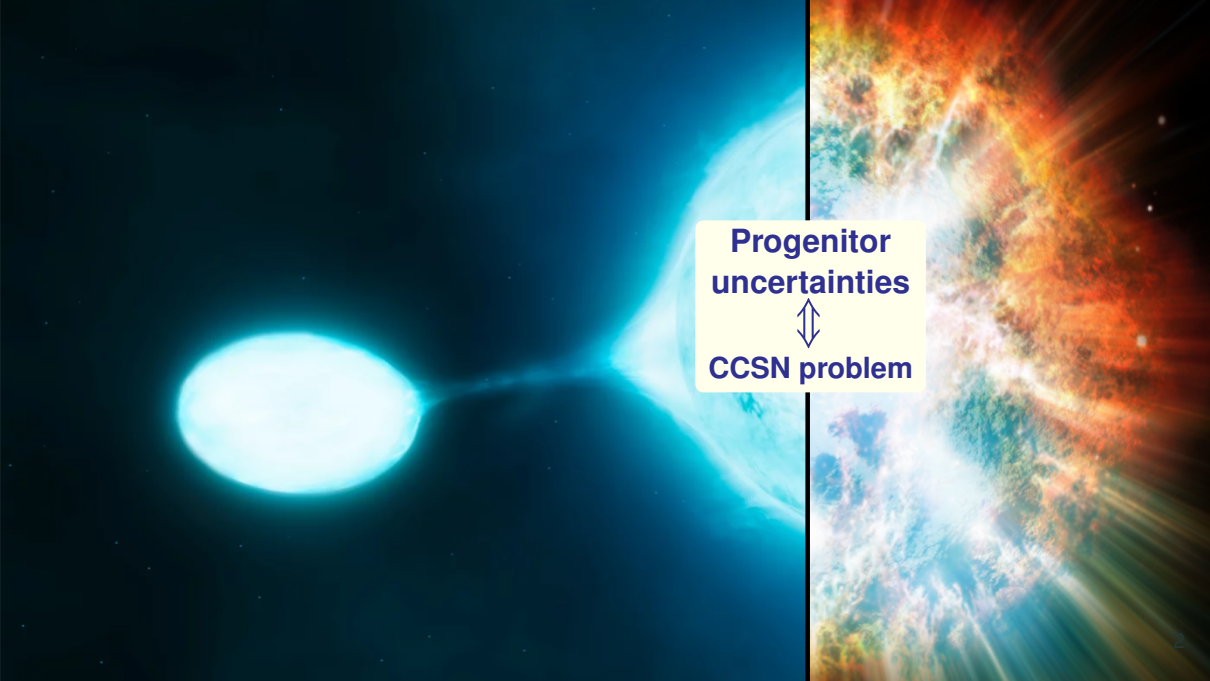
Binary Supernova Progenitors and why we haven't yet produced large grids

Mathieu Renzo

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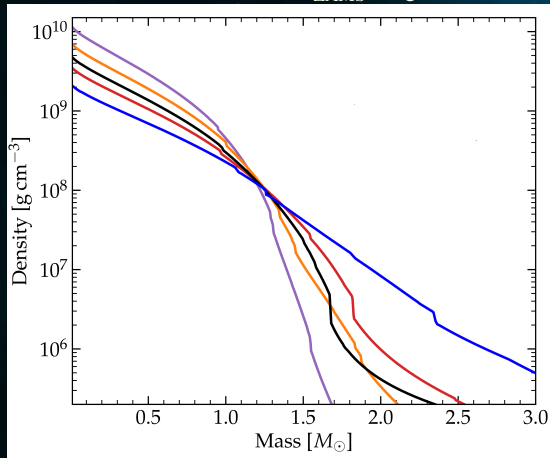


Collaborators: **A. Grichener, D. H. Hendriks, E. Farag, T. Wagg,**
E. Laplace, D. Vartanyan, J. Goldberg, E. Zapartas, Y. Götberg, S. Justham,
L. van Son, O. Gottlieb, M. Cantiello, B. D. Metzger, S. E. de Mink, R. Farmer ...



**Progenitor
uncertainties**
⇕
CCSN problem

KEPLER 12 – 40 M_{ZAMS} single stars



from Woosley *et al.* 2002, 2007 as shown in Ott *et al.* 2018

Progenitor
uncertainties



CCSN problem

Core structure is set by late core burning

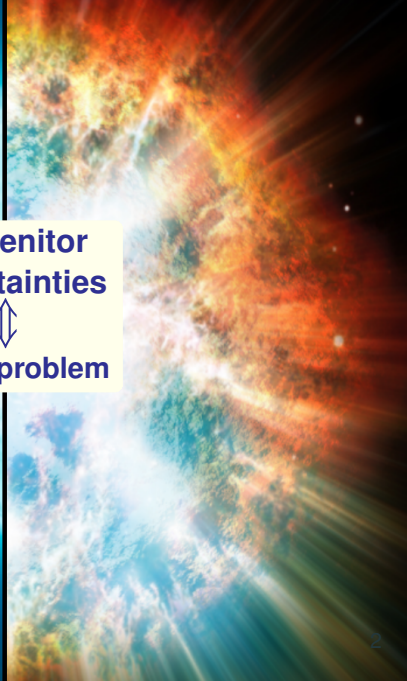
$$(\rho, Y_e) \Rightarrow (\dot{M}, L_{\nu_e}) \Rightarrow \text{“explodability”}$$


Kochanek 2009, O'Connor & Ott 2011, Ugliano *et al.* 2012, Sukhbold & Woosley 2014, Farmer *et al.* 2016, Ertl *et al.* 2016, 2020, Sukhbold *et al.* 2016, **Renzo *et al.* 2017**, Ott *et al.* 2018, Davies *et al.* 2019, Patton *et al.* 2020, 2021, Mandel & Müller 2020, **Laplace *et al.* 2021**, Vartanyan *et al.* 2021, 2023a, b, **Zapartas *et al.* 2017, 2019a,b, 2021**, Boccioli *et al.* 2022, Adams *et al.* 2017, Basinger *et al.* 2022, Beasor *et al.* 2023, Burrows *et al.* 1994, 2005, 2023, ...



**Progenitor
uncertainties**
⇕
CCSN problem

**Most progenitors we can see
are/were in binaries**





**Binaries and binary products
are unavoidable at population level**



Binary interactions create unique pre-SN structures

Podsiadlowski *et al.* 1989, 1990, 1991, Cantiello *et al.* 2007, Justham *et al.* 2014,
Renzo *et al.* 2020c, Schneider *et al.* 2020, 2021, 2023, Chatzopoulos *et al.* 2020, 2023,
Renzo & Götberg 2021, Laplace *et al.* 2021, 2023, Renzo *et al.* 2023, Henneco *et al.* 2023, ...

CCSN progenitors from binaries

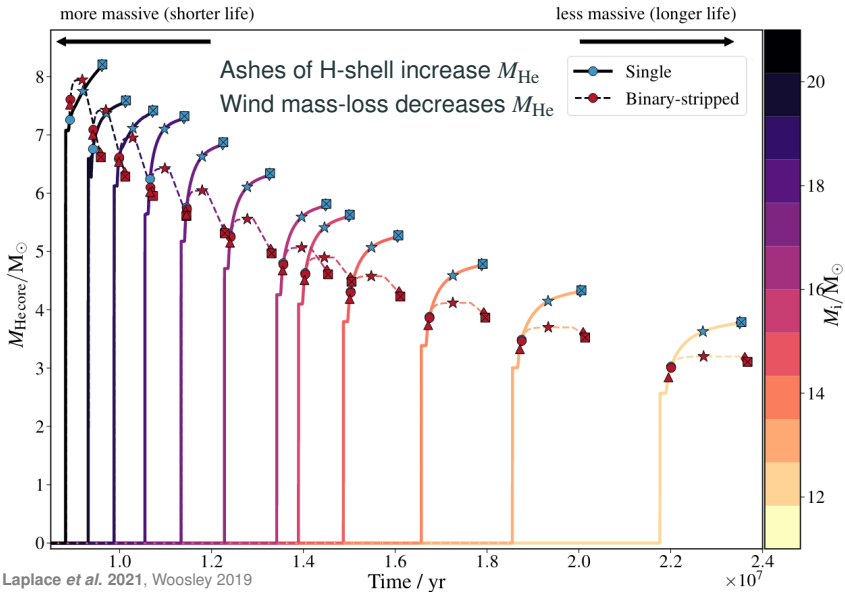
Donor

Accretor

Mergers (very massive ones)

Why no comprehensive answer (yet)

Donor: $M(t), J(t)$ influence He core burning ... and following phases



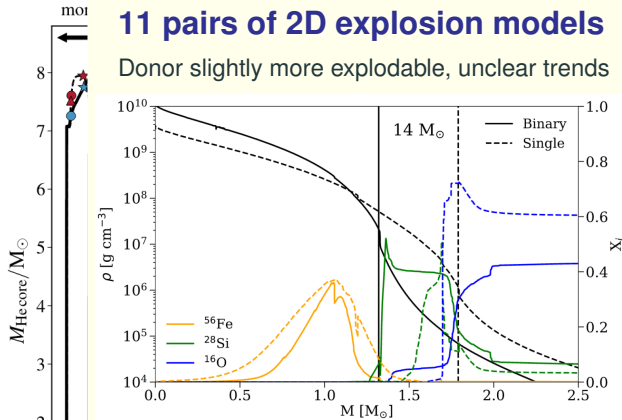
Donor vs. single



Donor: $M(t), J(t)$ influence He core burning ... and following phases

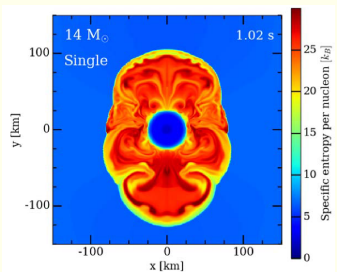
11 pairs of 2D explosion models

Donor slightly more explodable, unclear trends

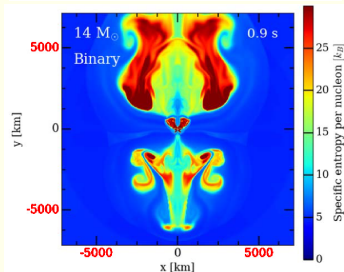


Vartanyan *et al.* 2021

Single



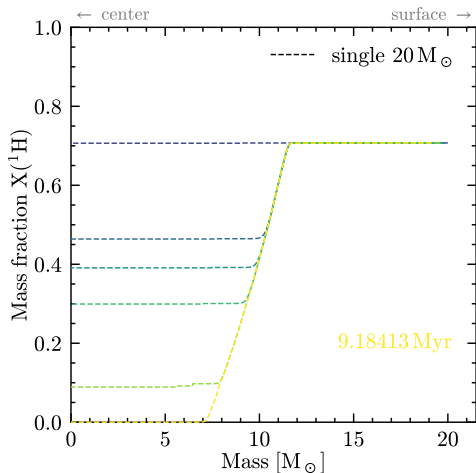
Donor



Single



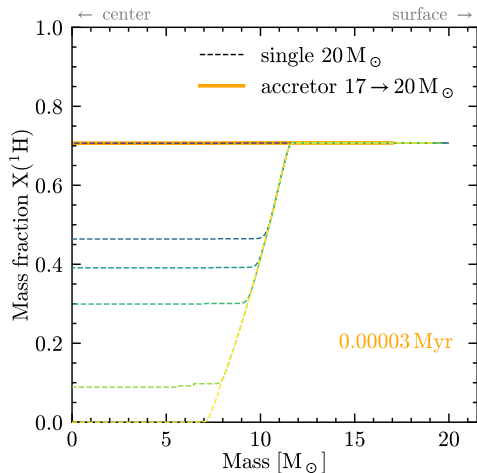
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



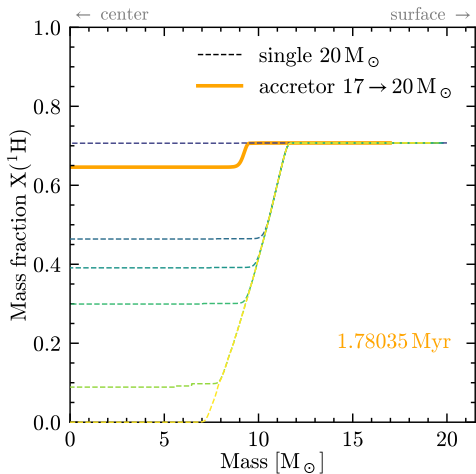
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



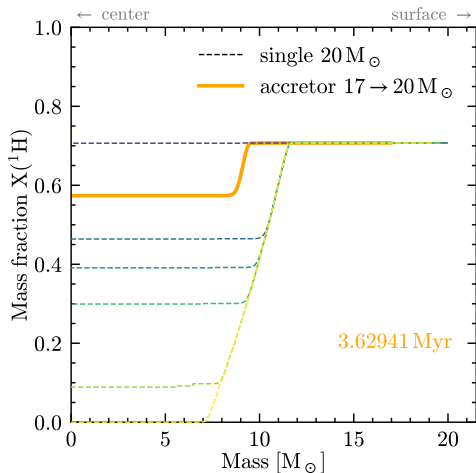
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



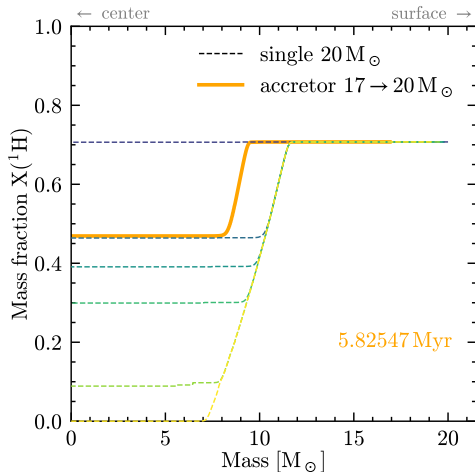
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



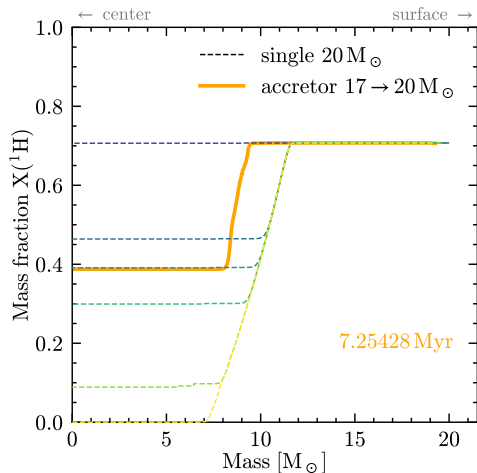
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



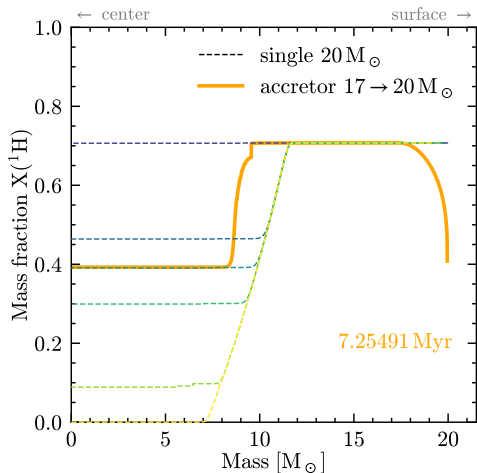
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



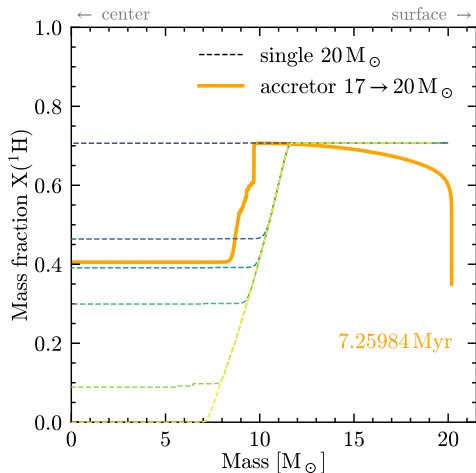
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



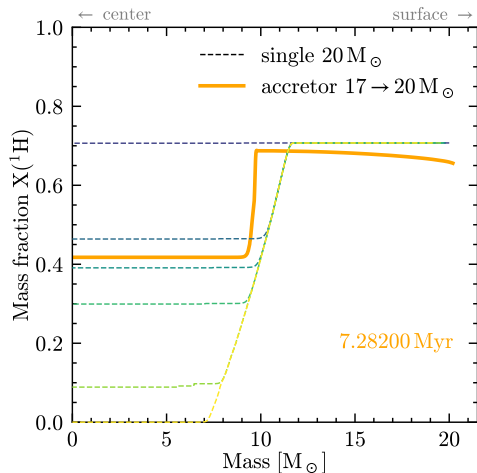
Accretor vs. single



Consequences

- Blue loops *Renzo et al. 2023*
- Lower envelope binding E *Renzo et al. 2023*
- long-GRB *Cantiello et al. 2007*

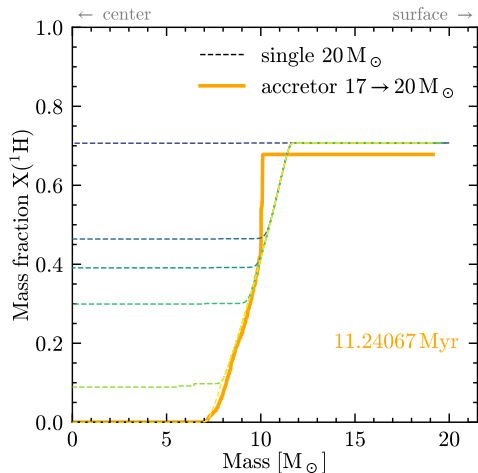
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



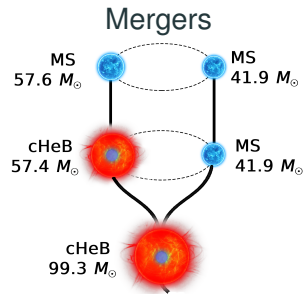
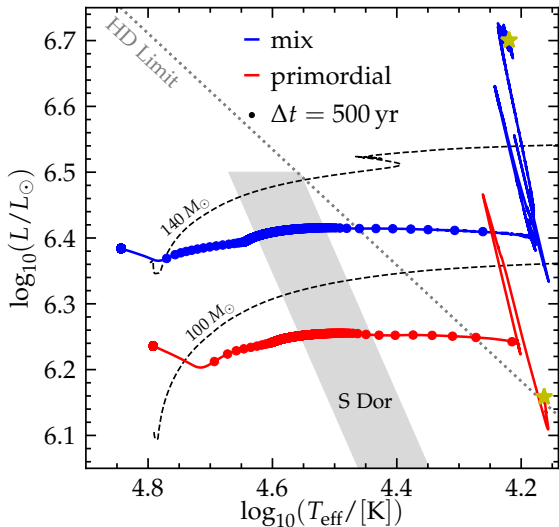
Accretor: $M(t)$, $J(t)$ influence He core burning ... and following phases



Accretor vs. single



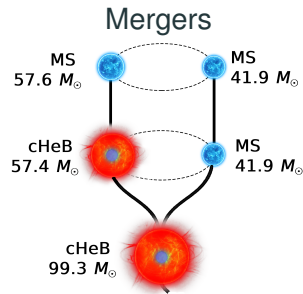
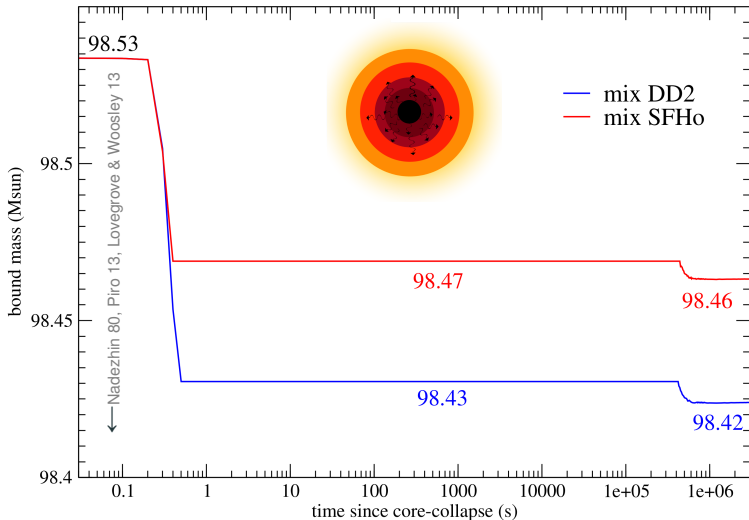
Mergers: $M(t)$, $J(t)$ influence He core burning ... and following phases



BH progenitors in the PISN gap?

Mergers: $M(t)$, $J(t)$ influence He core burning ... and following phases

MESA → GR1D+FLASH credits: R. Fernández



BH progenitors in the PISN gap?

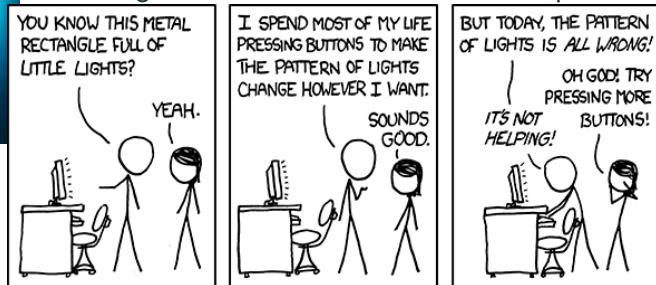
Exploration of binary “explodability” landscape not yet possible



Variety of evolutionary paths

- Orbital architecture M_1, M_2, P, e
- Z , winds, rotation, overshooting, ...
- Pre-/post-main sequence interactions
- Donors, Accretors, Mergers, Reversed-mergers

Getting one model to the onset of collapse:



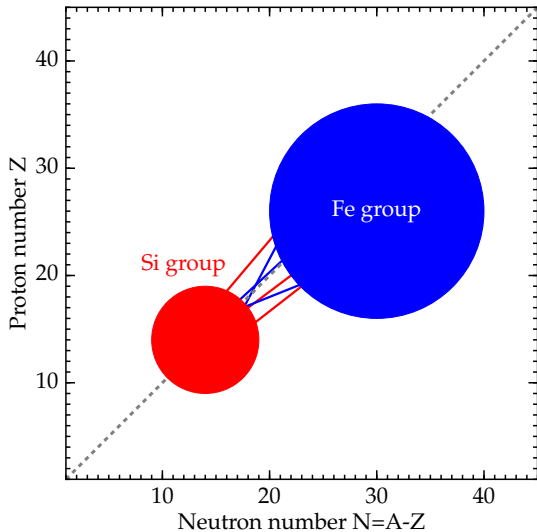
xkcd.com/722

Numerical challenges

(for single & binary progenitors)

Nuclear reaction networks
Input physics \Rightarrow C/O ratio
Spurious envelope velocities

Limiting factor: Post-carbon burning stiffness and numerical stability



Numerical techniques:

- “Compound” reactions

e.g., MESA code, Timmes *et al.* 1996

- Sub-timestep integration

e.g., MESA code, Paxton *et al.* 2011-2019, Jermyn *et al.* 2022

- Co-processing

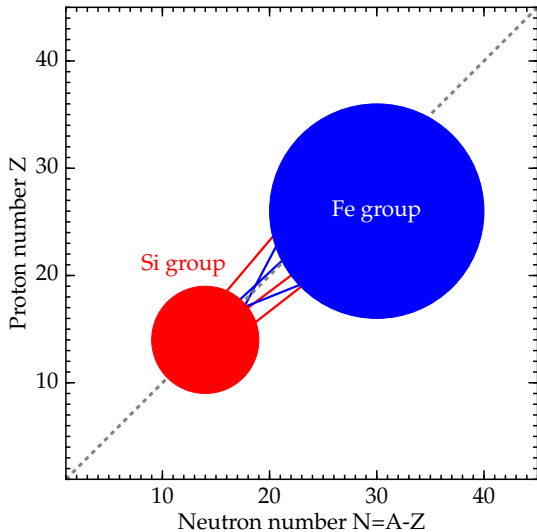
e.g., KEPLER code ???, Weaver *et al.* 1976,

FRANEC code???, Limongi & Chieffi 2013, 2018

- “Quasi” statistical equilibrium

Hix & Thielemann 1996, José & Iliadis 2011

Limiting factor: Post-carbon burning stiffness and numerical stability



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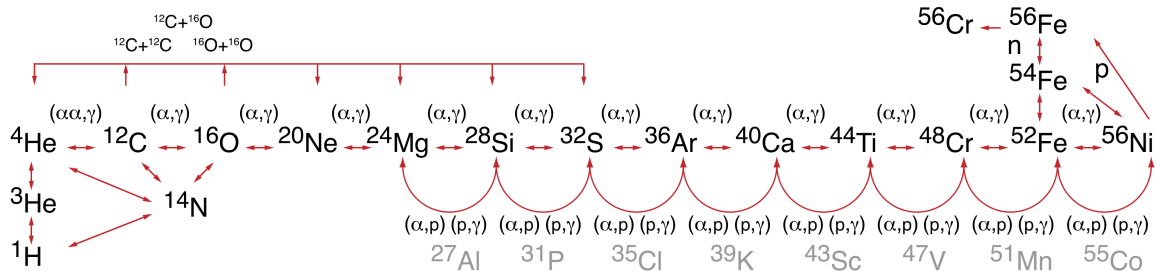
- Co-processing

e.g., KEPLER code ???, Weaver *et al.* 1976,
FRANEC code???, Limongi & Chieffi 2013, 2018

- “Quasi” statistical equilibrium

Hix & Thielemann 1996, José & Iliadis 2011

“Compound” reactions: α -chain nuclear reaction networks

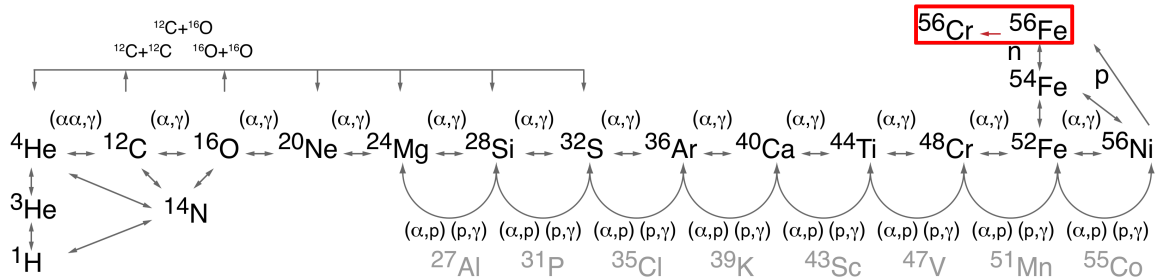


default in **MESA**

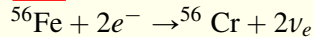
`approx21.net` $\Rightarrow N_{\text{iso}} = 21$

$\text{cost} \propto (N_{\text{mesh}} \times N_{\text{iso}})^2 \times N_{\Delta t}$

“Compound” reactions: α -chain nuclear reaction networks



The only weak reaction included

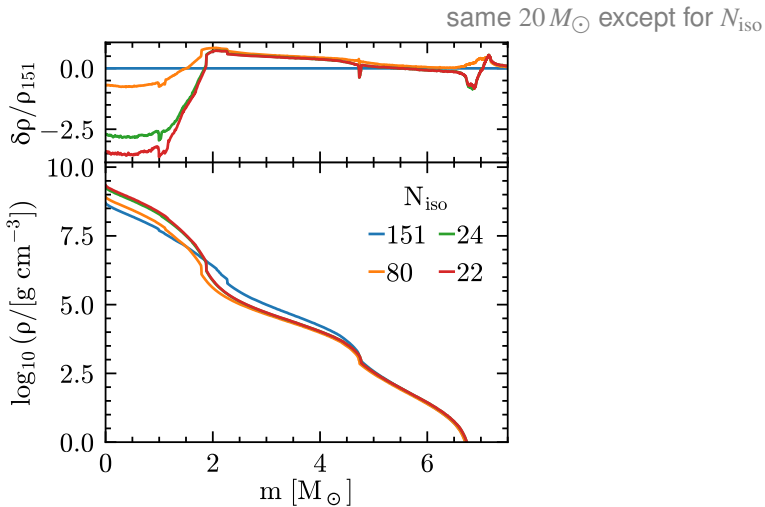


The core Y_e is pre-determined:

$$Y_e(r=0) \equiv Y_e({}^{56}\text{Cr}) = 0.428$$

Different nuclear network \Rightarrow different progenitor

MESA



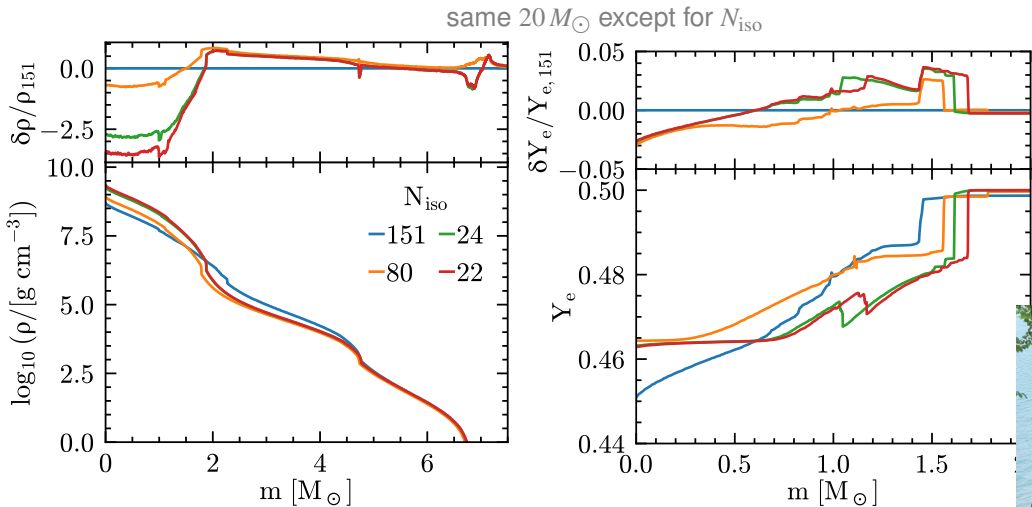
Aldana Grichener
(Technion)



N.B.: not yet converged with increasing N_{iso}

Different nuclear network \Rightarrow different progenitor

MESA



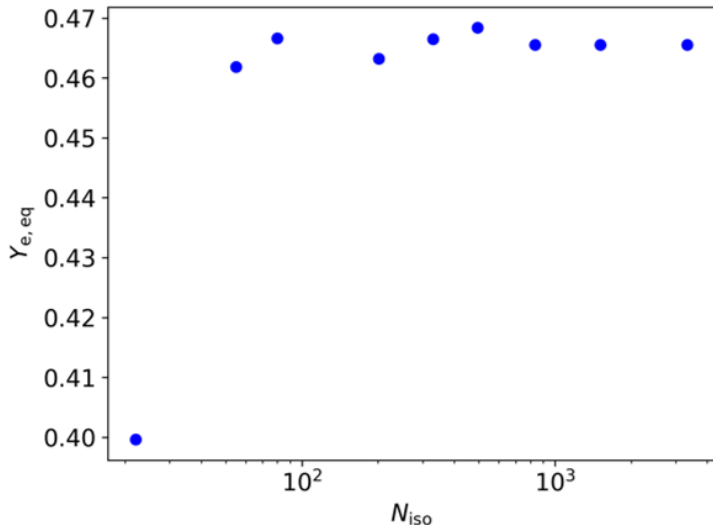
Aldana Grichener
(Technion)



N.B.: not yet converged with increasing N_{iso}

How many (and which) isotopes do we need?

Standalone MESA one-zone burner at fixed $\log_{10}(T/K) = 9.84$, $\log_{10}(\rho/[\text{g cm}^{-3}]) = 8.47$

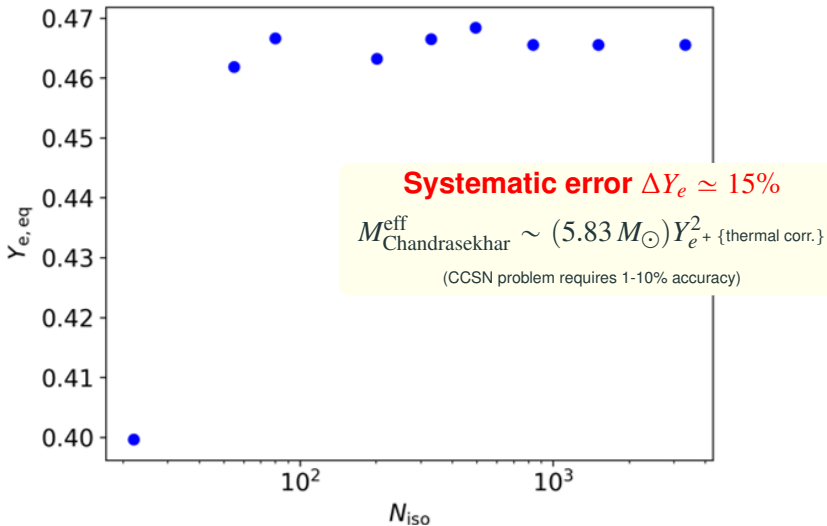


Aldana Grichener
(Technion)



How many (and which) isotopes do we need?

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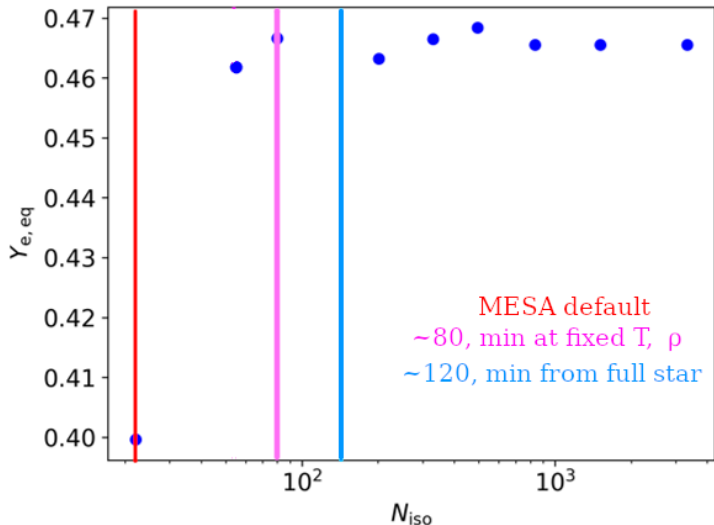


Aldana Grichener
(Technion)



How many (and which) isotopes do we need?

Standalone MESA one-zone burner at fixed $\log_{10}(T/K) = 9.84$, $\log_{10}(\rho/[g\text{ cm}^{-3}]) = 8.47$



CCSN progenitor are expensive!

$$\text{cost} \propto (N_{\text{mesh}} \times N_{\text{iso}})^2 \times N_{\Delta t}$$

Aldana Grichener
(Technion)

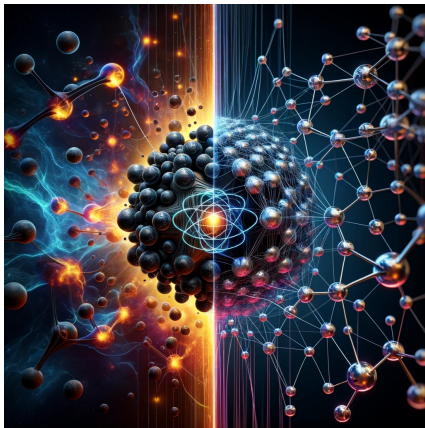


**Nuclear reaction networks
are the computational bottleneck but
not the dominant uncertainty[†]**

[†] cf. binary interactions, wind mass loss, rotation, convective boundary mixing, ...

Neural Nuclear Network: emulate away the nuclear reaction network

- ✓ Training set standalone *MESA* one-zone burner at fixed (T, ρ)
- Design and train neural-network to emulate $f : \mathbb{R}^{\sim 123} \rightarrow \mathbb{R}^{\sim 121}$
 $(\{X_i\} \times T \times \rho \times \Delta t) \rightarrow (\{X_i\} \times \varepsilon_{\nu, \text{nuc}})$

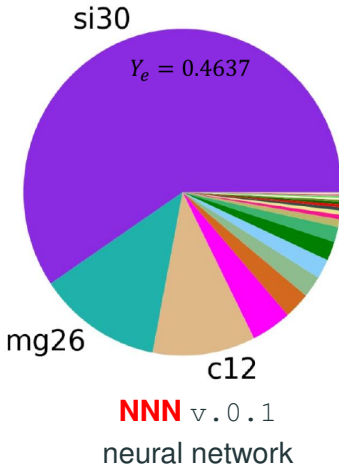
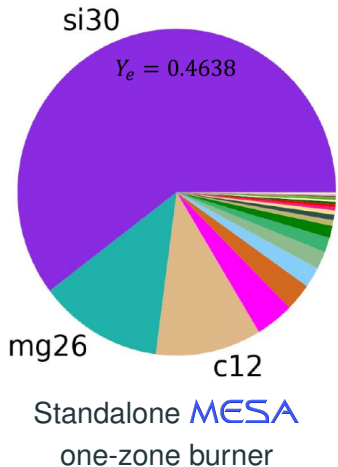


Dall-E generated by K. Wong

Aldana Grichener
(Technion)



Neural Nuclear Network: work in progress



Error: $\sim 4 - 131\%$

Aim: NNN for 1-,2-,3-D

Aldana Grichener
(Technion)

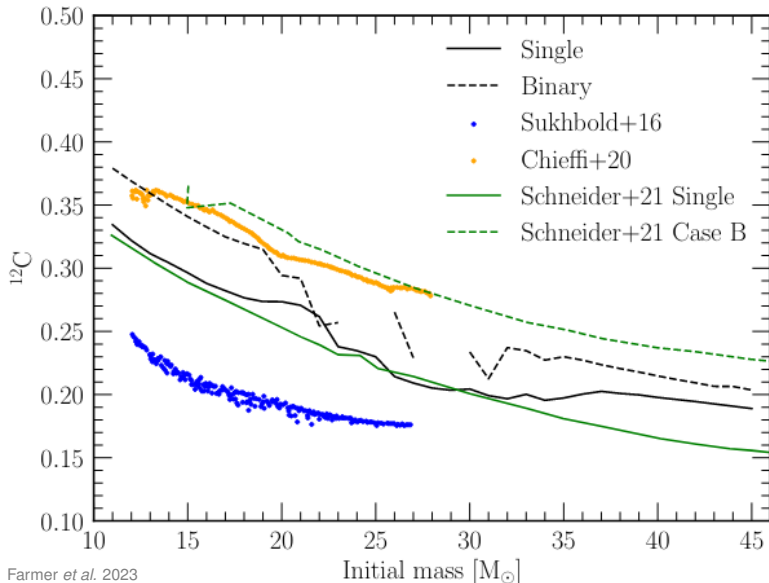


Numerical challenges

(for single & binary progenitors)

Nuclear reaction networks
Input physics \Rightarrow **C/O ratio**
Spurious envelope velocities

Core C/O ratio varies across models



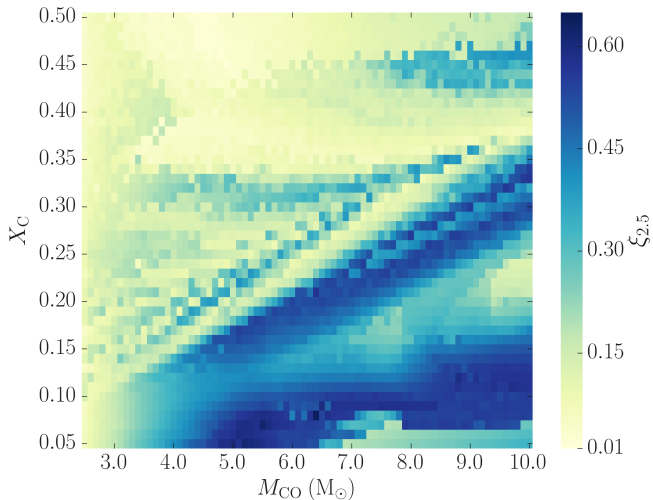
Set by T_c during (late) He core burning

- Code assumptions:
 - H/He core boundary
 - Wind mass loss
 - Rotational mixing
 - Nuclear rates
- Mass loss/accretion
 - case A/B RLOF

Adam may be right **not** to believe CO core masses
from nebular spectra

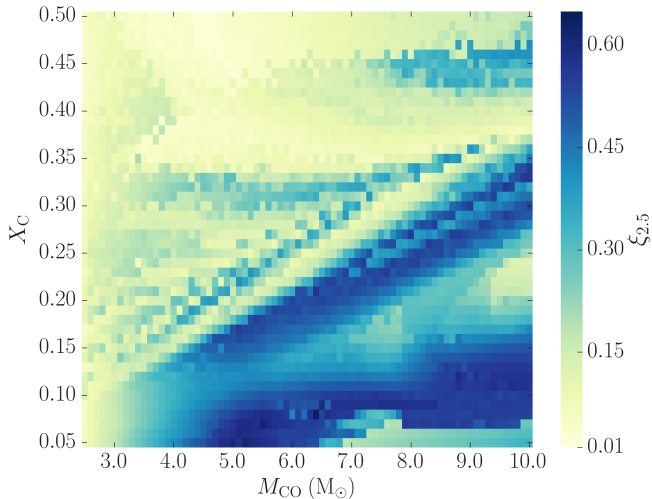
C/O ratio important for “explodability”

Pure CO cores evolved to pre-core-collapse



C/O ratio important for “explodability”

Pure CO cores evolved to pre-core-collapse



**No stripped-envelope SNe
from single stars:**

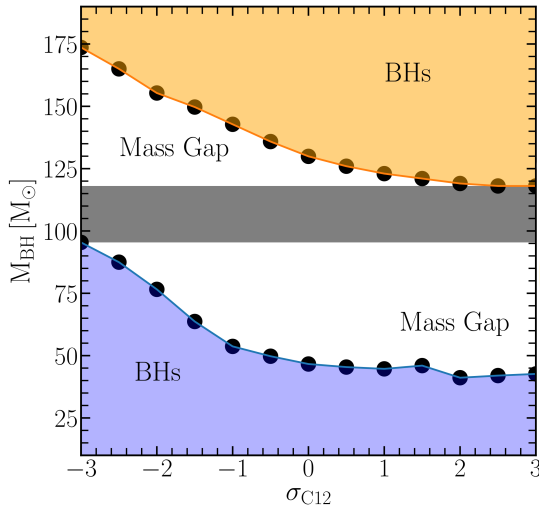
Massive enough for wind
self-stripping



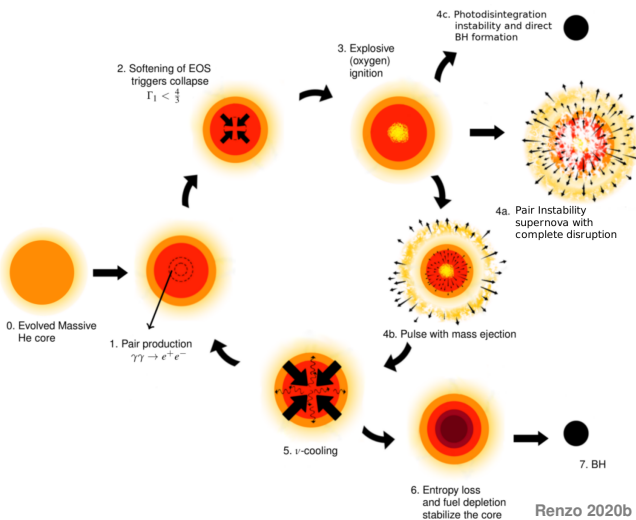
Too massive to explode

POSYDON (MESA)+KEPLER, Zapartas, Renzo, *et al.* 2021

$^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate key for (Pulsational) Pair Instability

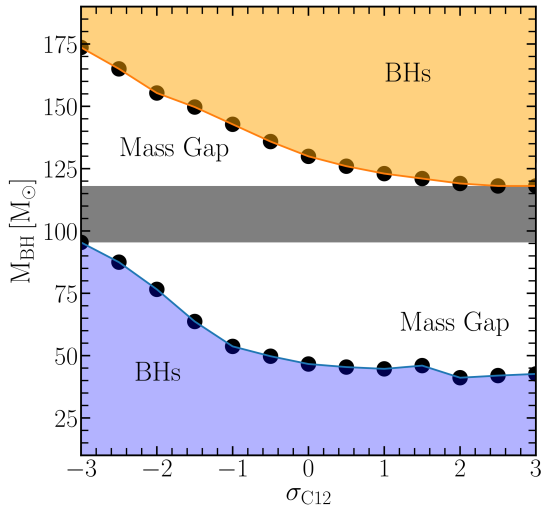


← lower Rate higher →

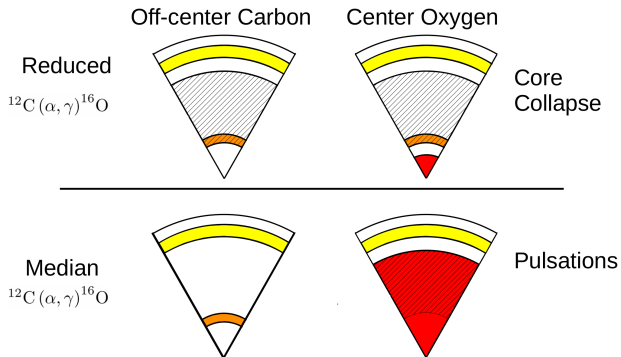


Renzo 2020b

Higher C/O \Rightarrow thicker C shell \Rightarrow stabilizing effect

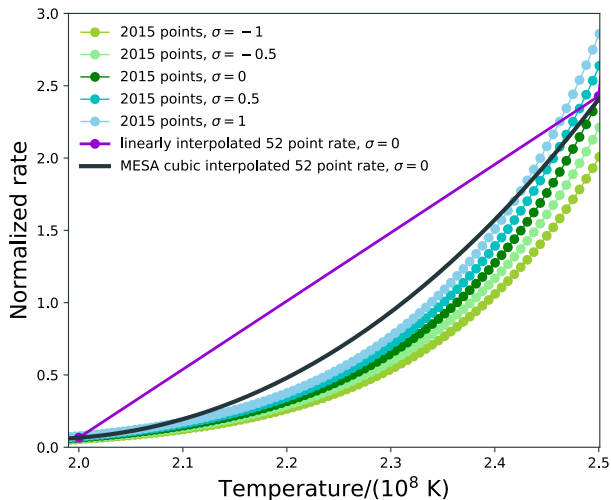
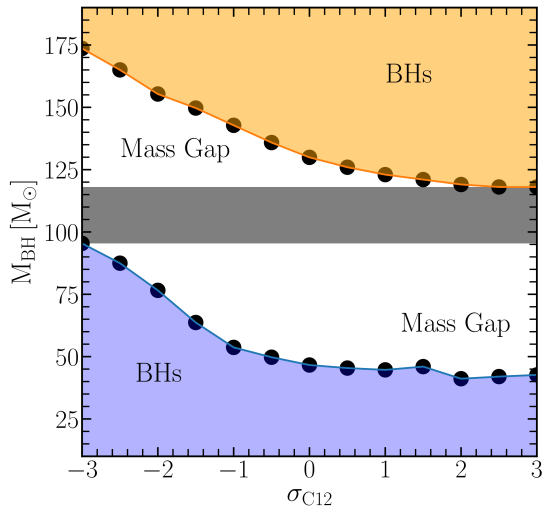


\Leftarrow lower **Rate** higher \Rightarrow



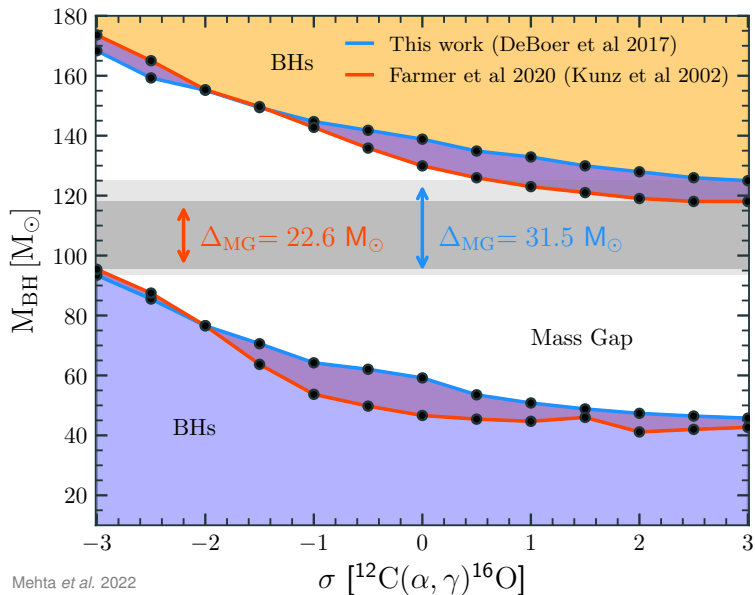
Farmer, Renzo *et al.* 2020, Woosley & Heger 2021
 Qualitatively similar for CCSN progenitors
 see also Sukhbold & Woosley 2014, Schneider *et al.* 2020, 2023

$^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate was undersampled in publicly available tables



← lower **Rate** higher ⇒

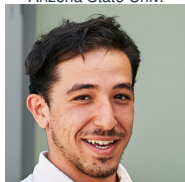
BH mass gap from single He cores with updated $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ rate



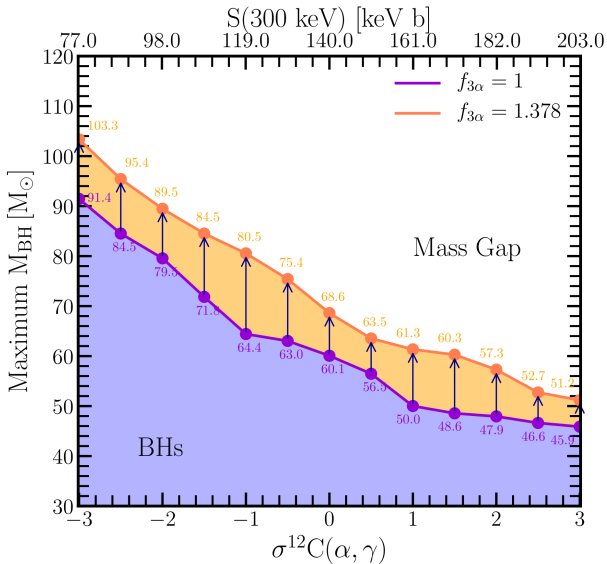
✓ Open science success!

- Open-source codes and SDK
- Input & output files on zenodo.org
- Refine tabulated input physics
- Community-driven improvements

Ebraheem "Eb" Farag
Arizona State Univ.



3 α rate uncertainties

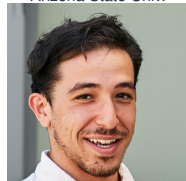


New edges of the gap:

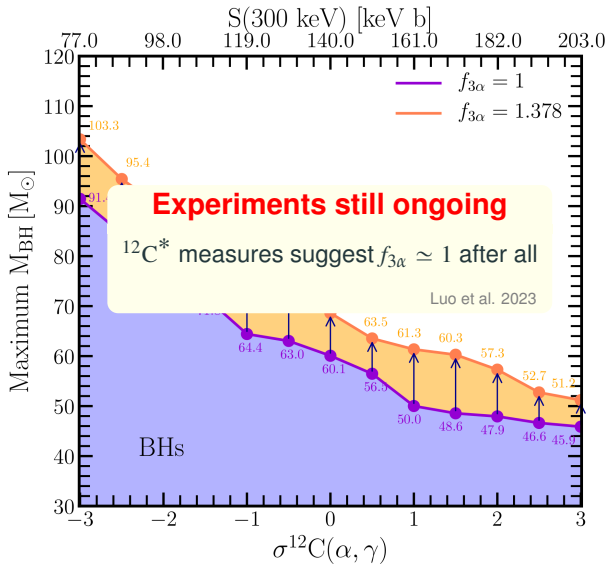
$\max(M_{\text{BH}})$ below the gap: $69^{+34}_{-18} M_{\odot}$

$\min(M_{\text{BH}})$ above the gap: $139^{+30}_{-14} M_{\odot}$

Ebraheem "Eb" Farag
Arizona State Univ.



3α rate uncertainties: ongoing debate!

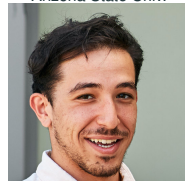


New edges of the gap:

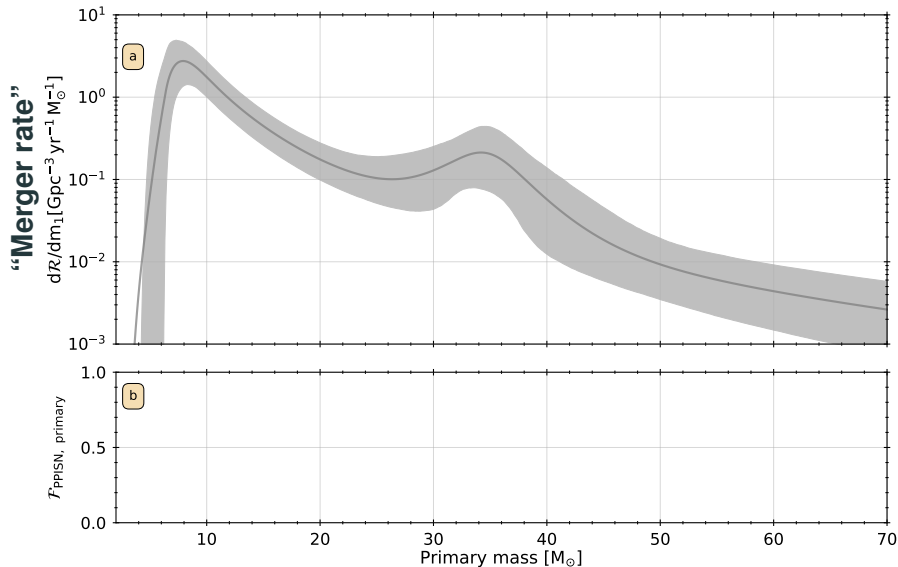
$\max(M_{\text{BH}})$ below the gap: $69^{+34}_{-18} M_{\odot}$

$\min(M_{\text{BH}})$ above the gap: $139^{+30}_{-14} M_{\odot}$

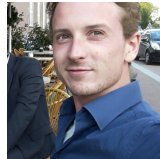
Ebraheem "Eb" Farag
Arizona State Univ.



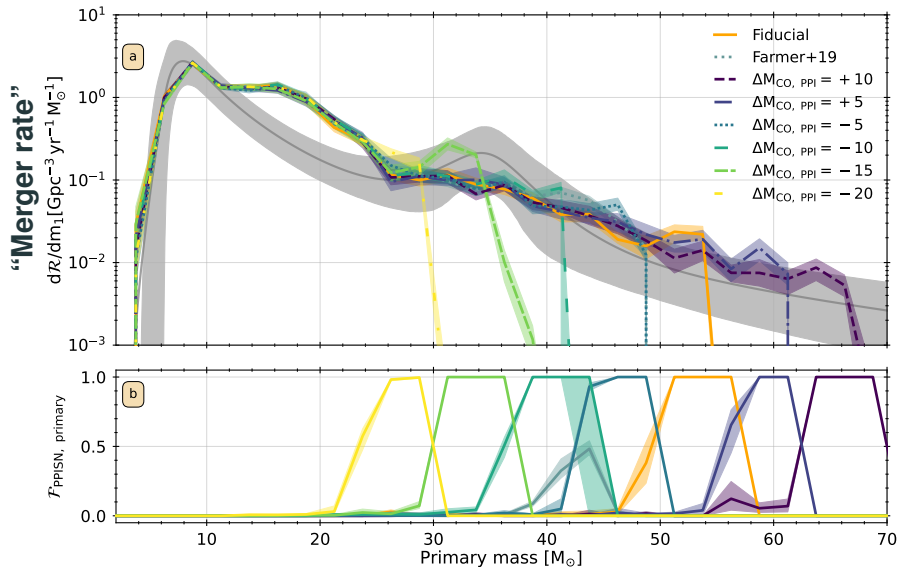
GW detected BHs: feature at $\sim 35 M_{\odot}$ and tail “in the gap”



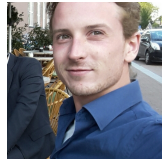
David D. Hendriks
Univ. Surrey



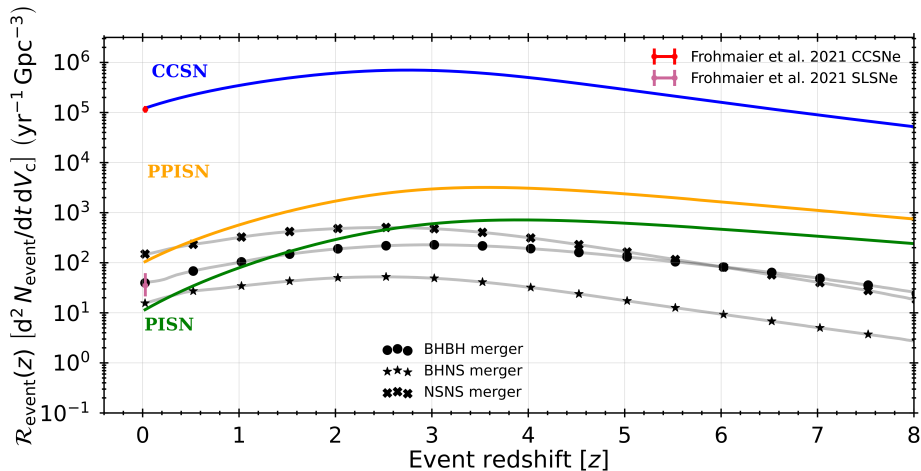
For $\sim 35 M_{\odot}$ feature to be related to (P)PISN requires $\Delta \min\{M_{\text{CO,PPI}}\} \simeq 15 M_{\odot}$



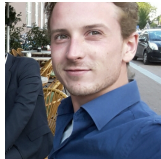
David D. Hendriks
Univ. Surrey



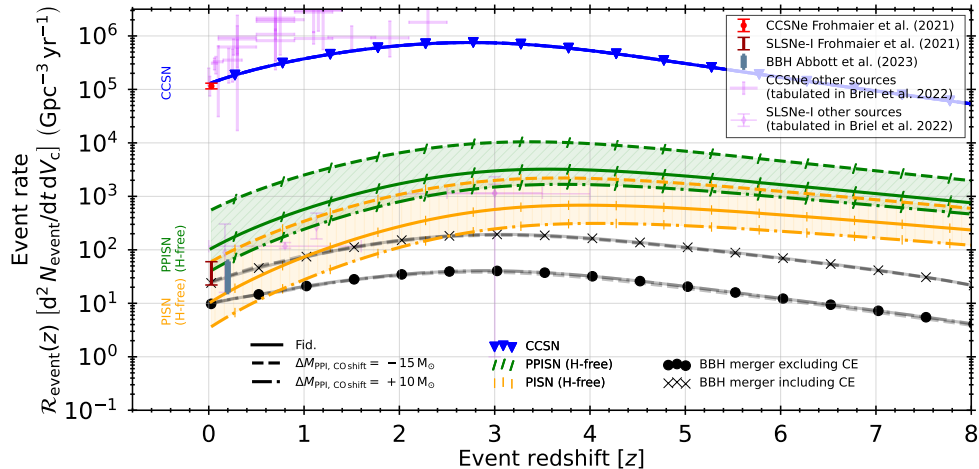
Combining GW and EM constraints increases the tension



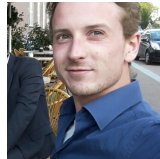
David D. Hendriks
Univ. Surrey



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Univ. Surrey

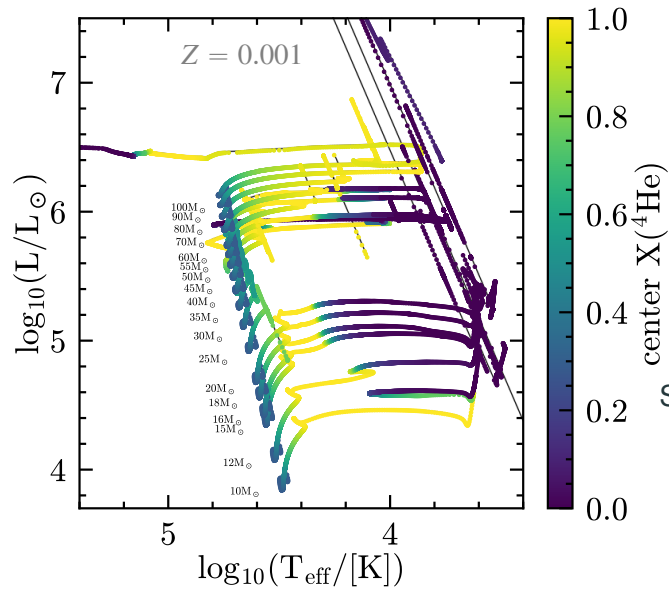


Numerical challenges

(for single & binary progenitors)

Nuclear reaction networks
Input physics \Rightarrow C/O ratio
Spurious envelope velocities

Late evolution results in $\nu/\dot{\nu} \ll \tau_{\text{dyn}}$ across the Hertzsprung-Russell diagram



Stellar engineering solutions:

- Damp/expunge “outer” ν

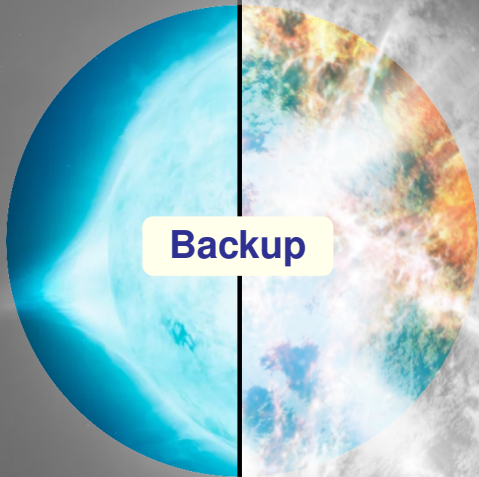
e.g., Farmer *et al.* 16, Renzo *et al.* 17, Aguilera-Dena *et al.* 18

- “stellar lid” by increasing P_{surf}

Conclusions

Progenitor uncertainties dominate the CCSN problem

- Most progenitors are born in binaries
and
Binary products are unavoidable in observations
- Binary evolution produces unique progenitors:
 - $M_{\text{core}}/M_{\text{env}}, J(m) \rightarrow$ explodability, BH/NS, jets, obs. diagnostic, yields
 - RSG vs. BSG vs. WR
 - delay time, location relative to SFR
 - ...
- ✗ Computational challenges prevent exploring the parameter space
 - Core structure \rightarrow leverage ML
 - Envelope stability \rightarrow “stellar engineering”
missing relevant physics?
- $\sim 35 M_{\odot}$ feature in BH mass from GWs **not** from (P)PISN



Backup

Formal definition of “stiffness”

A set of Ordinary Differential Equations is “stiff” if:

$$\frac{\max(\mathbb{E}(\mathcal{J}))}{\min(\mathbb{E}(\mathcal{J}))} \in \mathbb{C}$$

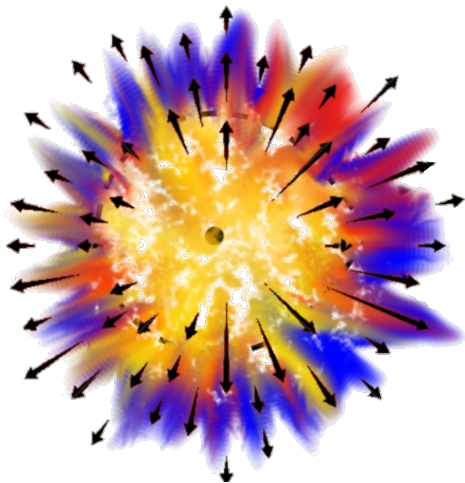
and

$$\frac{|\max(\mathbb{E}(\mathcal{J}))|}{|\min(\mathbb{E}(\mathcal{J}))|} \gg 1$$

where $\mathbb{E}(\mathcal{J})$ are the eigenvalues of the Jacobian matrix of the system:

$$\mathcal{J}_{ij} = \frac{\partial f_i}{\partial x_j}$$

Do BHs form via a failed, weak, or full blown SN explosion?



$$\Delta E_\nu \simeq 10^{53} \text{ erg}$$

Possible causes for mass ejection at BH formation:

- ν -driven shocks

Nadhezin 1980, Lovegrove & Woosley 2014, Fernandez *et al.* 2018,
Ivanov & Fernandez 2021

- Jets and disk wind

(even without net rotation)

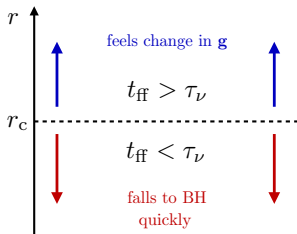
Gilkis & Soker 2014, Perna *et al.* 2018, Quataert *et al.* 2019

- (weak) fallback powered explosion

Ott *et al.* 2018, Kuroda *et al.* 2018, Chan *et al.* 2020, Powell *et al.* 2021

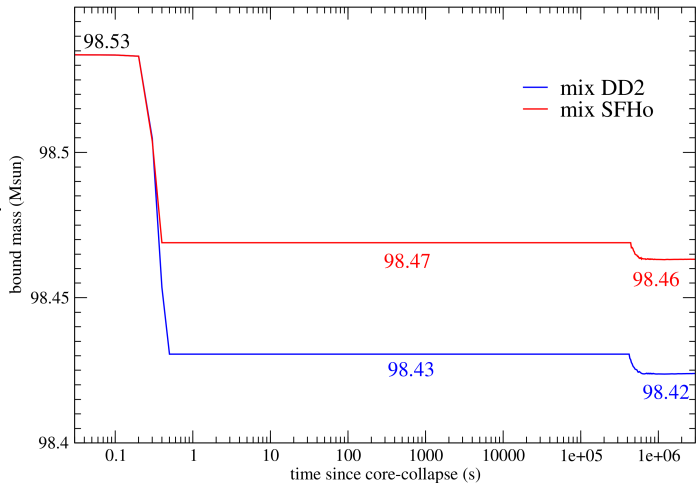
Accretion disks and ν -driven shocks remove little mass for BSG

$$M_{\text{BH},0} \simeq M_{\text{core}} - E_{\nu}/c^2$$

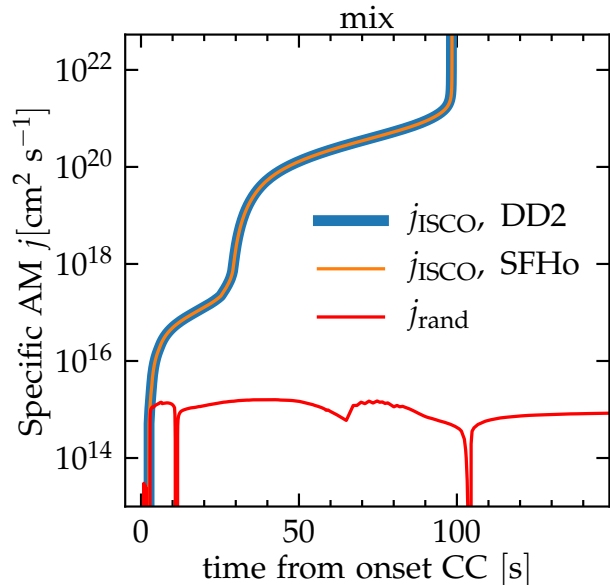


Fernández *et al.* 2018

MESA \rightarrow GR1D+FLASH credits: R. Fernández

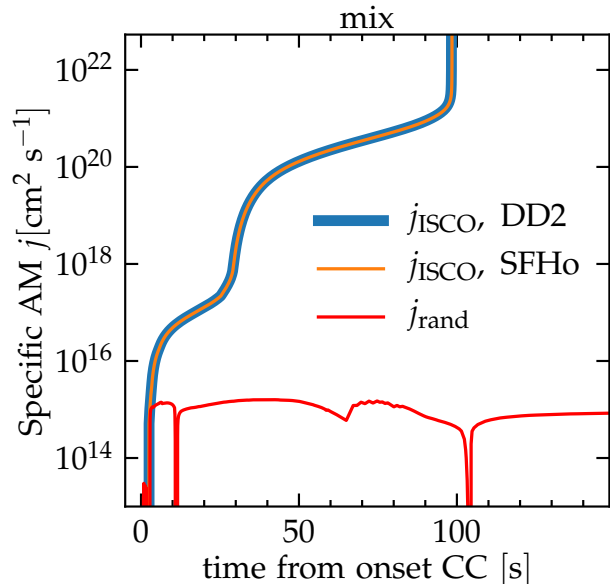


Can convective random motion cause disk formation and collapse?



$$j_{\text{rand}} = \frac{H_p v_{\text{conv}}}{\sqrt{4\pi}}$$

Can convective random motion cause disk formation and collapse?



$$\dot{j}_{\text{rand}} = \frac{H_p v_{\text{conv}}}{\sqrt{4\pi}}$$

Not enough in non-rotating models
But the merger process might inject AM

EM transients from (P)PISN

Approximate supernova type

(mass-loss dependent, Sec. 7)

Pulse delay to core-collapse

(Sec. 6)

Thermonuclear ignition

(Sec. 5.1)



Radial expansion

$\max R(v < v_{\text{esc}})$ (Sec. 5.2)



Number of mass ejections

(Sec. 5.3)



M_{CSM} He-rich

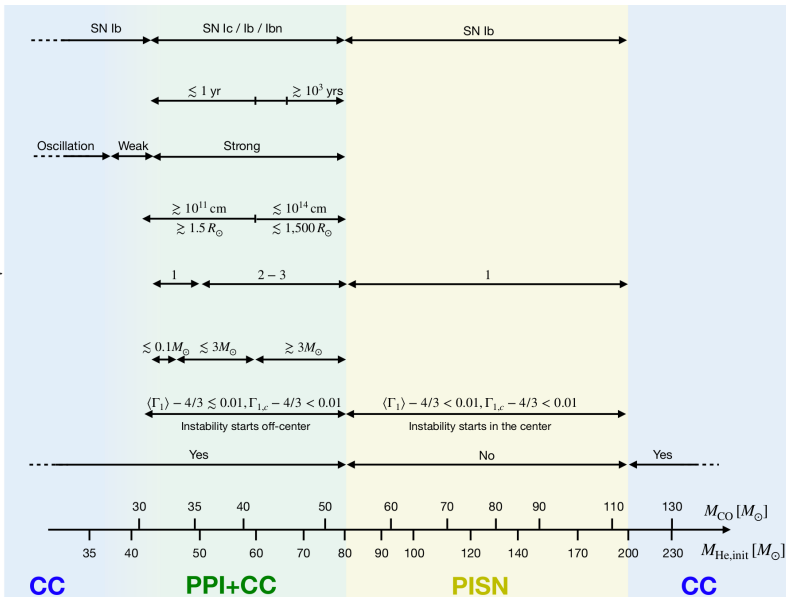
(Sec. 6)

Thermal stability

(Sec. 5.1.1)

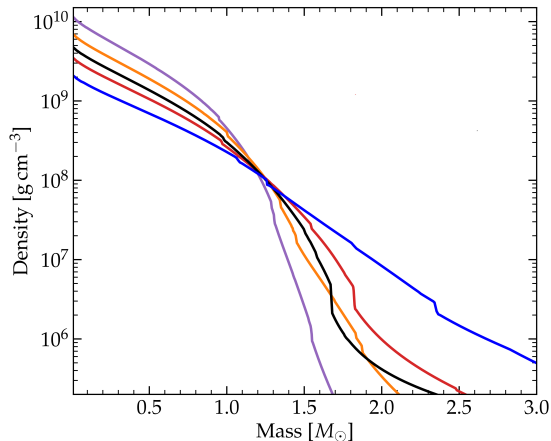
BH remnant

(Sec. 3)



SN success/failure is determined by progenitor core profile

KEPLER 12 – $40 M_{\text{ZAMS}}$ models



Core structure is set by late core burning

- $Y_e = \sum_i Z_i / (Z_i + N_i) \Rightarrow \nu$ flux
- $\rho \Rightarrow (\dot{M}, L_{\nu_e}) \Rightarrow$ “explodability”

from Woosley *et al.* 2002, 2007 as shown in Ott *et al.* 2018

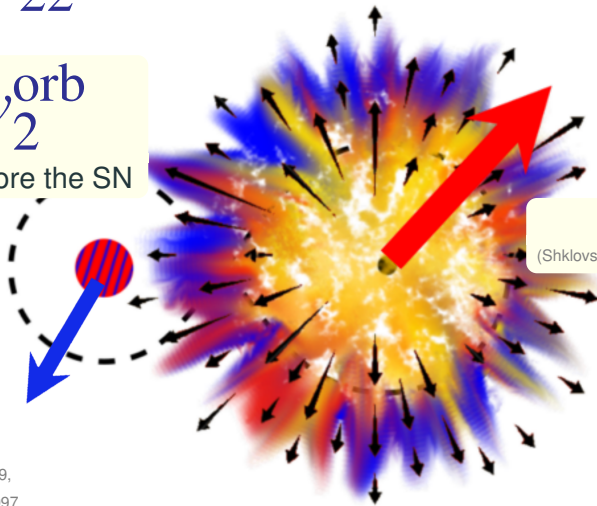
Kochanek 2009, O'Connor & Ott 2011, Ugliano *et al.* 2012, Sukhbold & Woosley 2014, Farmer *et al.* 2016, Ertl *et al.* 2016, 2020, Sukhbold *et al.* 2016, Renzo *et al.* 2017, Ott *et al.* 2018, Davies *et al.* 2019, Patton *et al.* 2020, 2021, Mandel & Müller 2020, Laplace *et al.* 2021, Vartanyan *et al.* 2021, 2023a, b, Zapartas *et al.* 2017, 2019a,b, 2021, Baccioli *et al.* 2022, Adams *et al.* 2017, Basinger *et al.* 2022, Beasor *et al.* 2023, Burrows *et al.* 1994, 2005, 2023, ...

Accretors may live alone, **but they are *not* single stars**

$86^{+11}_{-22}\%$ of massive binaries are disrupted

$$v_{\text{dis}} \simeq v_{\text{orb}}^{\text{orb}}$$

before the SN

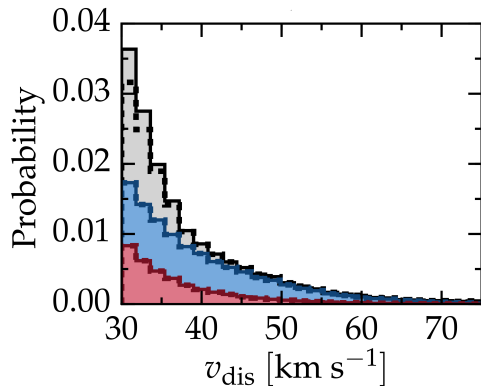


SN Natal kick

(Shklovskii 1970, Katz 1975, Janka 2013, 2017)

Kinematics of the widowed stars

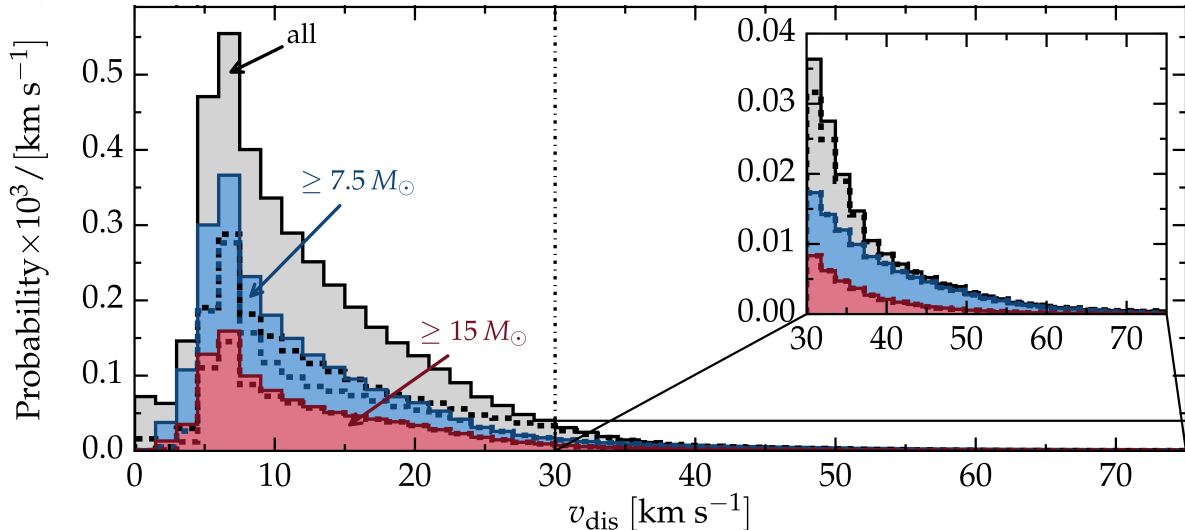
Accretor stars can be *runaways*...



Velocity w.r.t. pre-explosion binary center of mass

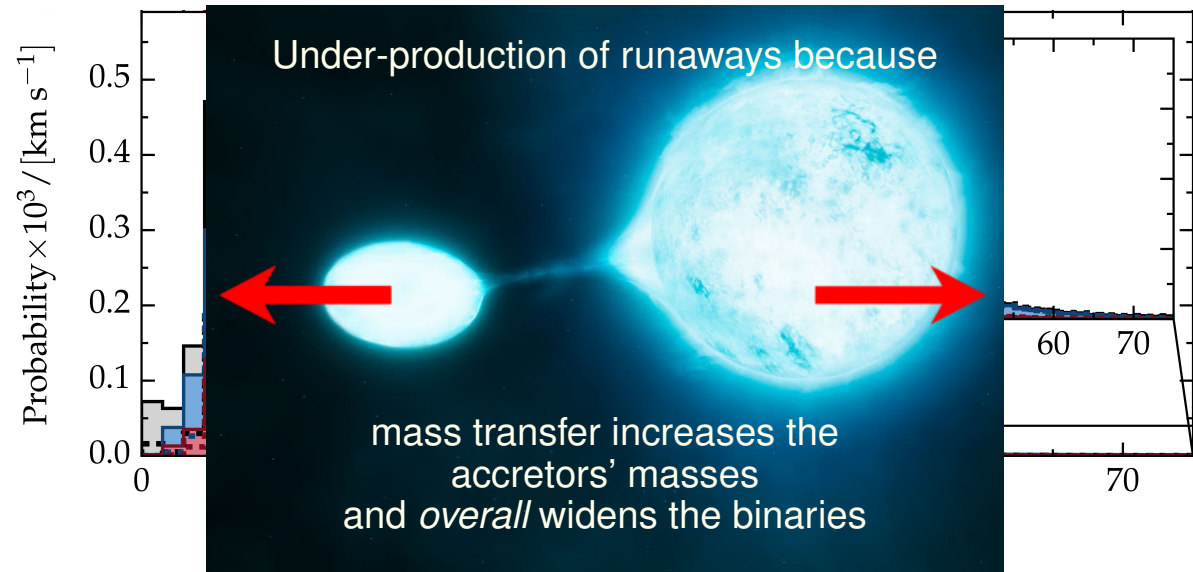
Numerical results: <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/624/A66>

...but most are only *walkaways*



Velocity w.r.t. pre-explosion binary center of mass

...but most are only *walkaways*



Structure of accretors

- Spin-up

Packet 1981, Cantiello *et al.* 2007, de Mink *et al.* 2013, Barker, Renzo *et al.*, in prep.

- Pollution

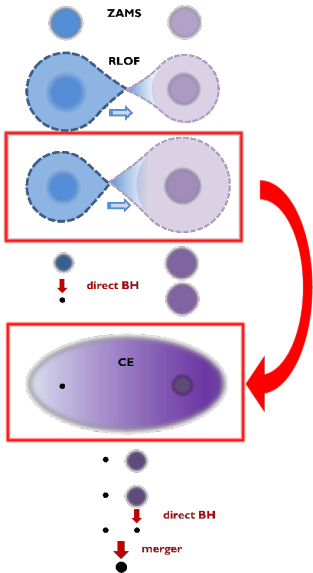
Blaauw 1993, Renzo & Götberg 2021

- Rejuvenation

Hellings 1983, 1985, Renzo *et al.* 2023



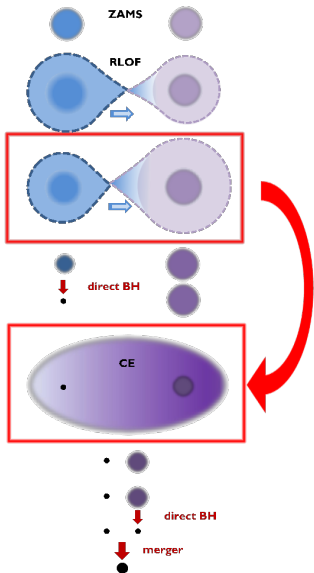
The common envelope in GW progenitors is initiated by the accretor



Does RLOF rejuvenation impact how easy it is to remove the envelope ?

Renzo *et al.* 2023

The common envelope in GW progenitors is initiated by the accretor

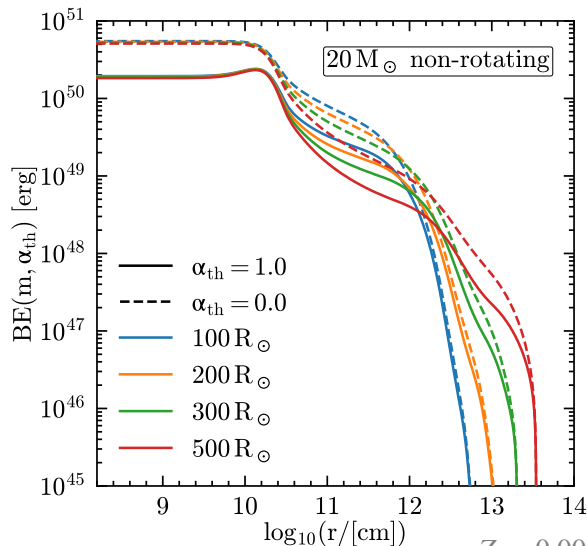


Does RLOF rejuvenation impact how easy it is to remove the envelope ?

Renzo *et al.* 2023

1. Binary evolution until detachment
2. Continue evolution of accretors as single stars
3. Compare **binding energy** of accretors and single stars of same total mass at given R

The binding energy is the cost to “dig” into the star



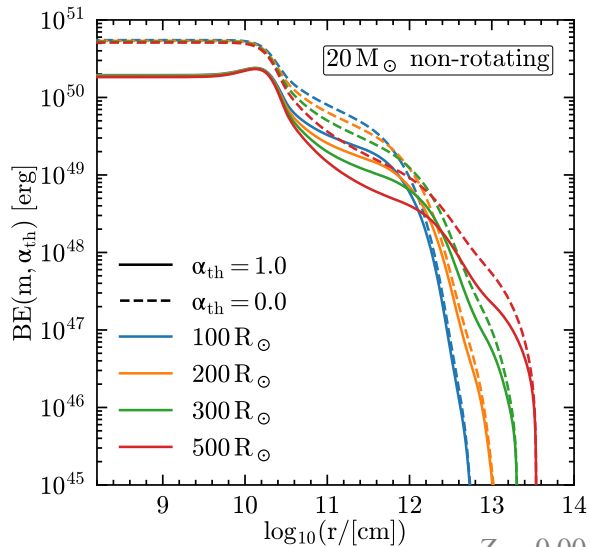
$$BE(m, \alpha_{\text{th}}) = - \int_m^M dm' \left(-\frac{Gm'}{r(m')} + \alpha_{\text{th}} u(m') \right)$$

- Gravitational potential energy
- Internal energy
- α_{th} free parameter

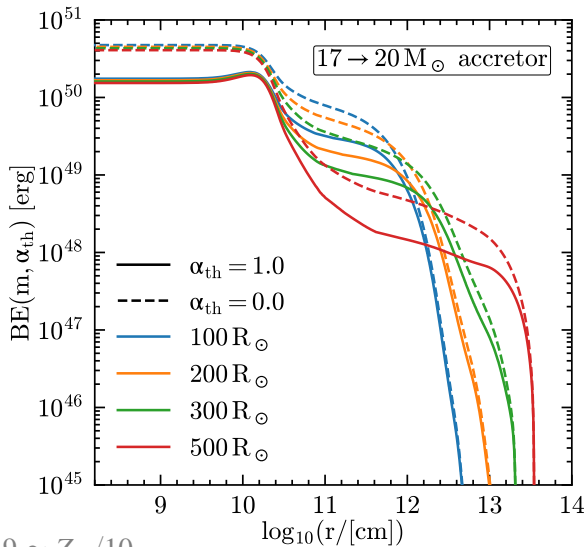
fraction of internal energy usable to eject envelope

$$Z = 0.0019 \simeq Z_{\odot}/10$$

Comparing $20 M_{\odot}$ non-rotating single star vs. accretor

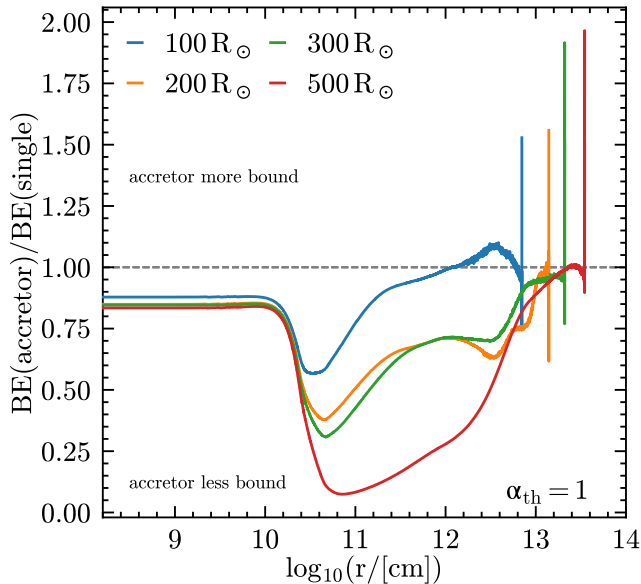


$Z = 0.0019 \simeq Z_{\odot}/10$



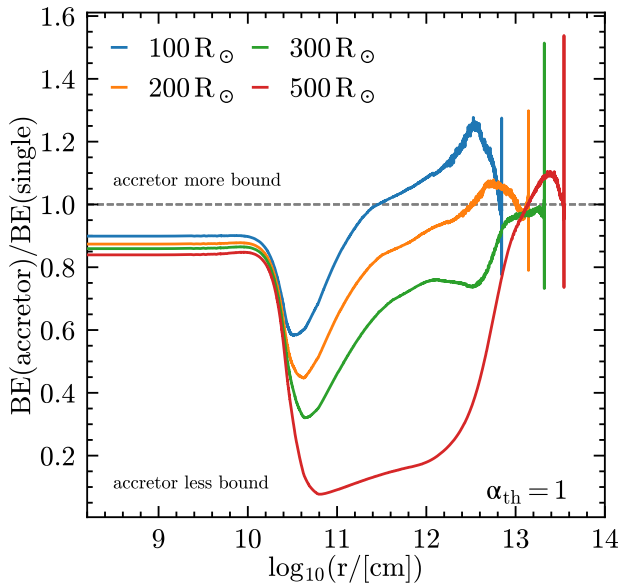
Taking the ratio: accretors are easier to unbind

NS progenitor
 $15 \rightarrow 17 M_{\odot}$



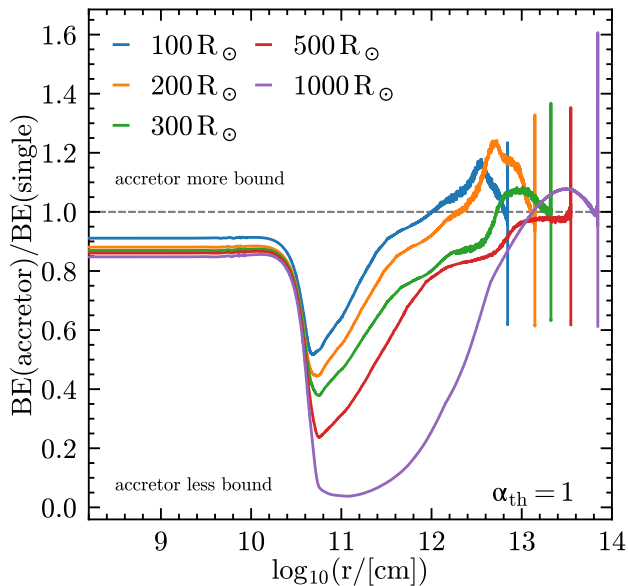
Taking the ratio: accretors are easier to unbind

NS or BH progenitor
 $17 \rightarrow 20 M_{\odot}$

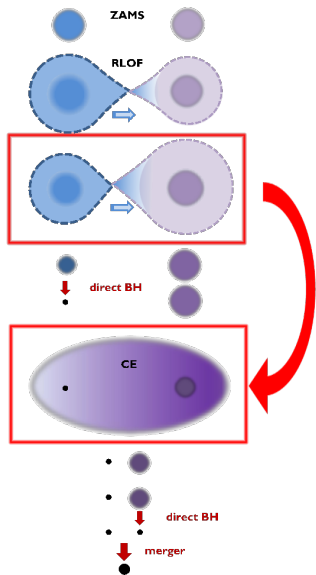


Taking the ratio: accretors are easier to unbind

BH progenitor
 $30 \rightarrow 36 M_{\odot}$



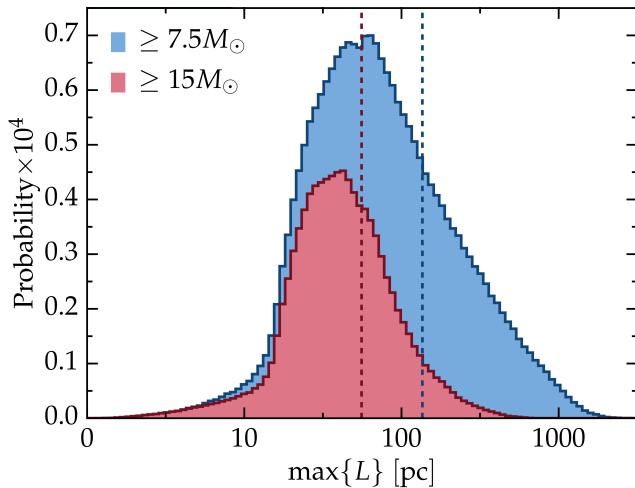
If the common-envelope donor is a former accretor



Implications for common-envelope

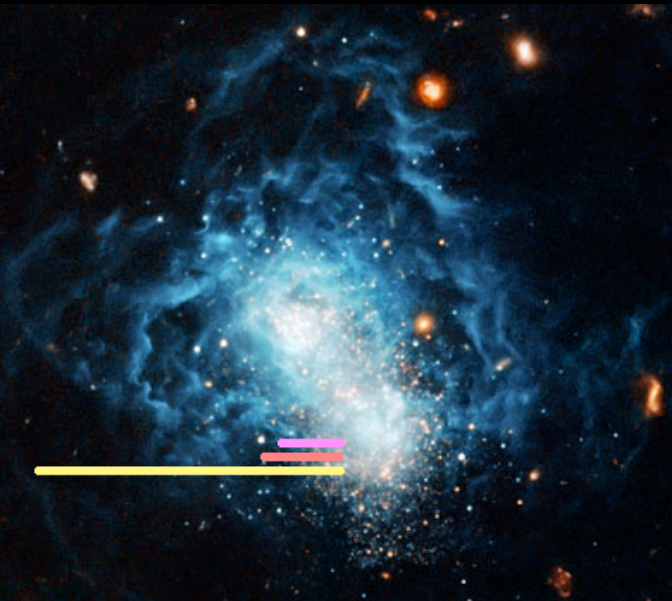
- Fewer “reverse” stellar merger
- Wider post-CE separation
- Mass-dependent (?) impact on GW merger rates

How far do they get?



“Distance traveled”
(No potential well)

Nevertheless: widowed stars can escape local dust clouds



for $M \geq 7.5 M_{\odot}$:

$$\langle D \rangle = 128 \text{ pc}$$

$$\langle D_{\text{run}} \rangle = 525 \text{ pc}$$

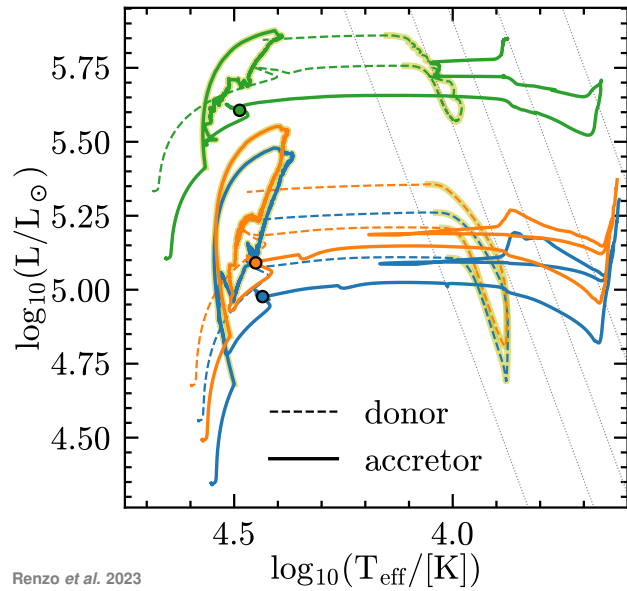
$$\langle D_{\text{walk}} \rangle = 103 \text{ pc}$$

Renzo *et al.* 19b

I Zw 18

Credits: ESA/Hubble & Nasa, A. Aloisi

Low-Z massive accretors



$$Z = 0.0019 \simeq Z_{\odot}/10$$

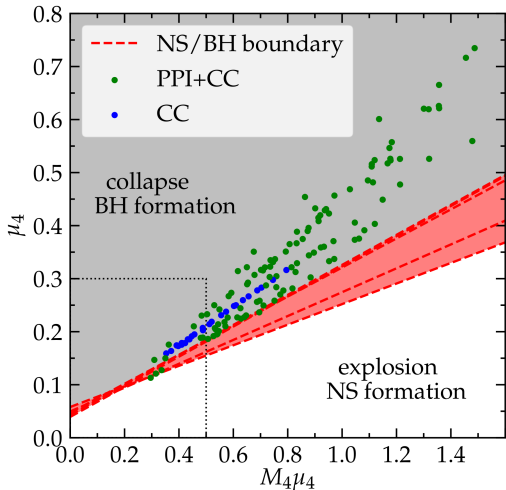
(to focus on GW merger progenitors)

PPISN explodability

Population synthesis implementation

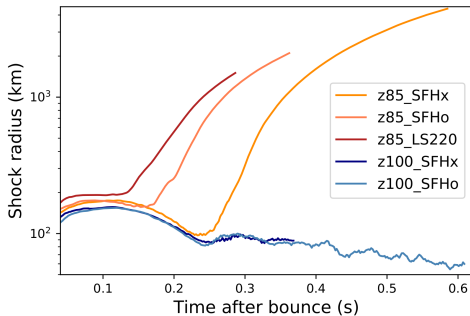
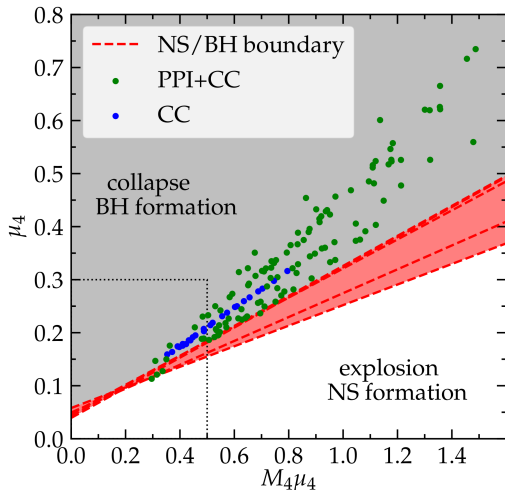
Can the final core-collapse result in an explosion?

Parametric 1D explodability criteria
are not really applicable.



Can the final core-collapse result in an explosion?

Parametric 1D explodability criteria
are not really applicable.



Powell, Müller, Heger 2021

$\max \Delta M_{\text{CC}} \lesssim 3.5 M_{\odot}$
from ν -driven engines

Rahman *et al.* 2021

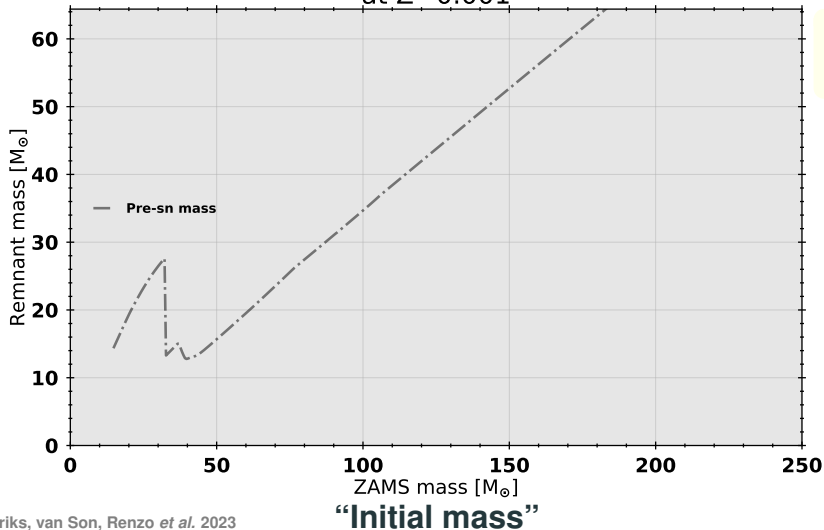
PPISN explodability

Population synthesis implementation

Population synthesis: $M_{\text{initial}} \rightarrow \text{CO core mass}^\dagger \rightarrow \text{BH mass}$

† and composition! (Patton & Sukhbold 2020)

Black hole remnant mass distribution for single star evolution
at $Z=0.001$



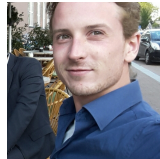
Fryer *et al.* 2012

see also Fryer *et al.* 22, Olejak *et al.* 22

see also:

Belczynski *et al.* 2016, Spera & Mapelli 2017, Stevenson *et al.* 2019, Mandel & Müller 2020, van Son *et al.* 2021, Renzo *et al.* 2022, Farag *et al.* 2022 ...

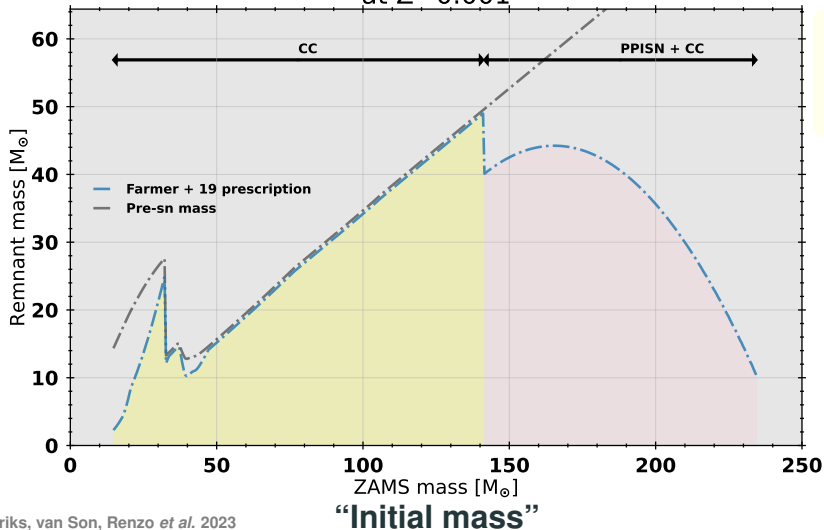
David D. Hendriks
Univ. Surrey



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Fryer *et al.* 2012

+

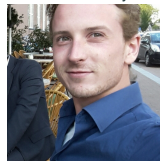
Farmer *et al.* 2019

see also:

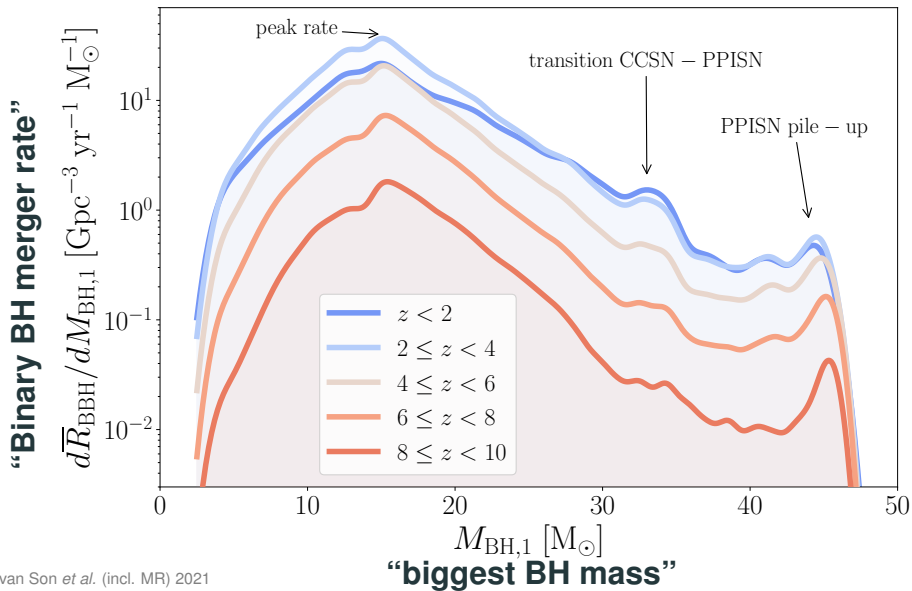
Belczynski *et al.* 2016, Spera & Mapelli 2017, Stevenson *et al.* 2019, Mandel & Müller 2020, van Son *et al.* 2021, Renzo *et al.* 2022, Farag *et al.* 2022 ...

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Univ. Surrey



Using “recipes” out-of-the-box leads to artificial features



Pair-instability mass loss for top-down compact object mass calculations

M. RENZO,^{1,2} D. D. HENDRIKS,³ L. A. C. VAN SON,^{4,5,6} AND R. FARMER⁶

¹*Center for Computational Astrophysics, Flatiron Institute, New York, NY 10010, USA*

²*Department of Physics, Columbia University, New York, NY 10027, USA*

³*Department of Physics, University of Surrey, Guildford, GU2 7XH, Surrey, UK*

⁴*Center for Astrophysics | Harvard & Smithsonian, 60 Garden St., Cambridge, MA 02138, USA*

⁵*Anton Pannekoek Institute for Astronomy, University of Amsterdam, Science Park 904, 1098XH Amsterdam, The Netherlands*

⁶*Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Straße 1, 85741 Garching, Germany*

$$M_{\text{BH}} = M_{\text{proto-NS}} + M_{\text{fallback}}$$

(e.g., Fryer *et al.* 2012, 2022)



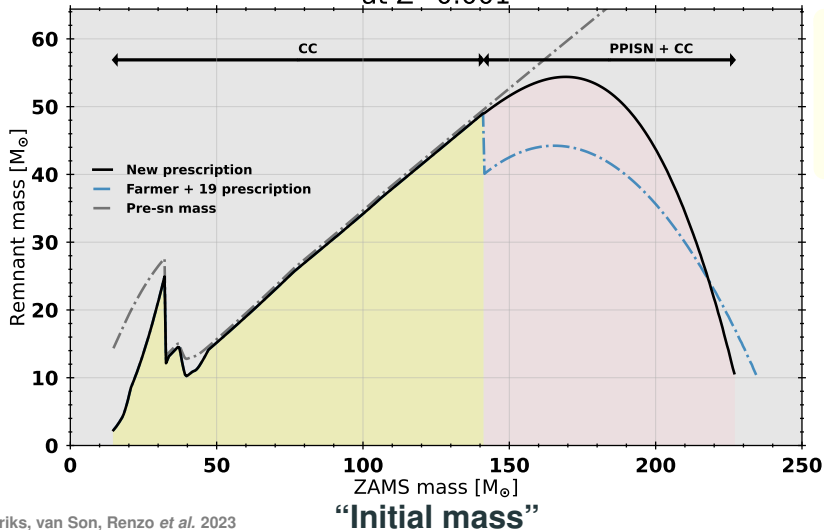
$$M_{\text{BH}} = M_{\text{pre-explosion}} - (\Delta M_{\text{SN}} + \Delta M_{\nu, \text{core}} + \Delta M_{\text{env}} + \Delta M_{\text{PPI}} + \dots)$$

New fit to **Farmer, Renzo *et al.* 2019**

Population synthesis: $M_{\text{initial}} \rightarrow \text{CO core mass} \rightarrow \text{BH mass}$

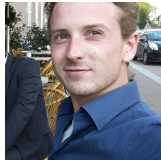
† and composition! (Patton & Sukhbold 2020)

Black hole remnant mass distribution for single star evolution at $Z=0.001$

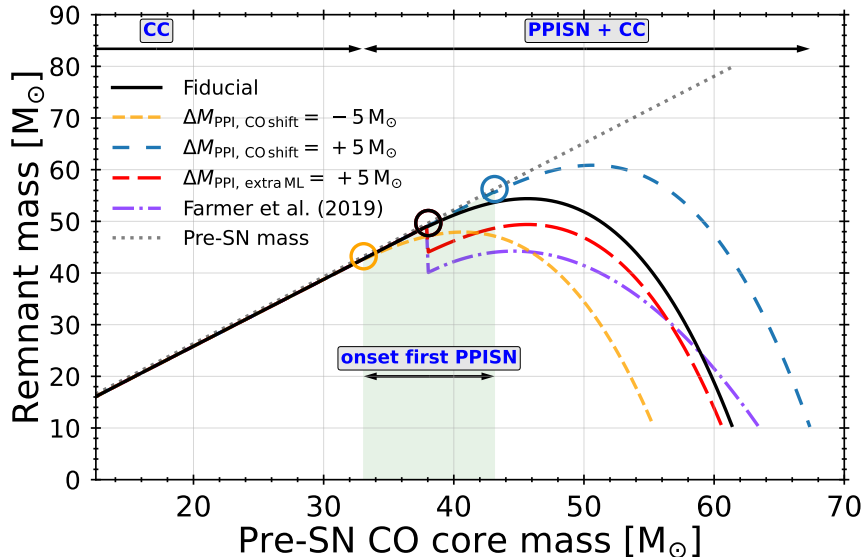


Fryer *et al.* 2012
+
Farmer *et al.* 2019
Renzo *et al.* 2022

David D. Hendriks
Univ. Surrey



Population synthesis: $M_{\text{initial}} \rightarrow$ CO core mass[†] \rightarrow BH mass
[†]and composition! (Patton & Sukhbold 2020)



Fryer *et al.* 2012

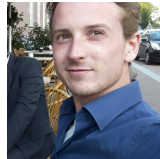
+

Farmer *et al.* 2019

Renzo *et al.* 2022

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“Classical” wisdom: core and envelope decouple late in the evolution

$$L_{\nu, \text{cooling}} \gg L_{\gamma}$$

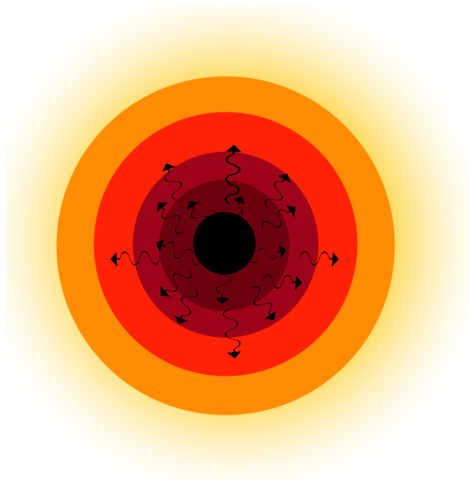
e.g., Fraley 1968



$$\tau_{\text{nuc}}(m \leq M_{\text{core}}) \ll \tau_{\text{KH}}$$



“Frozen-envelope”



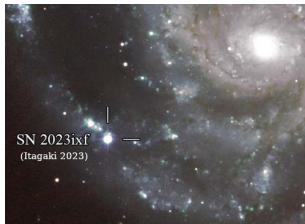
Observational evidence that core and envelope do **not** decouple

$$L_{V, \text{cooling}} \gg L_{\gamma}$$

e.g., Fraley 1968



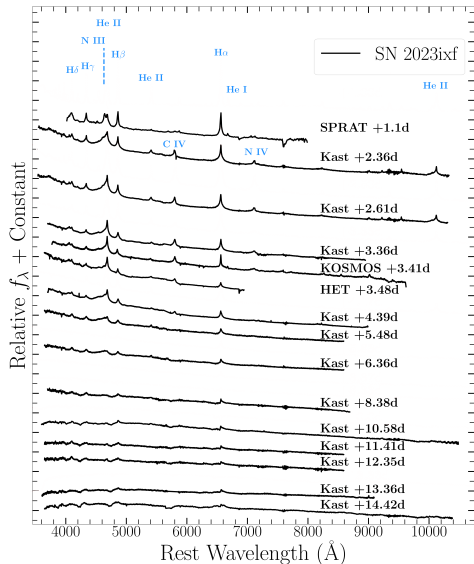
$$\tau_{\text{nuc}}(m \leq M_{\text{core}}) \ll \tau_{\text{KH}}$$



Late mass-ejection episodes are common

- $\gtrsim 36\%$ and possibly up to $\sim 50\%$ of type II SNe
- $\dot{M} \gtrsim 10^{-3} M_{\odot} \text{ yr}^{-1}$ within $10^2\text{--}3$ days pre-explosion
- Later SN looks “normal”

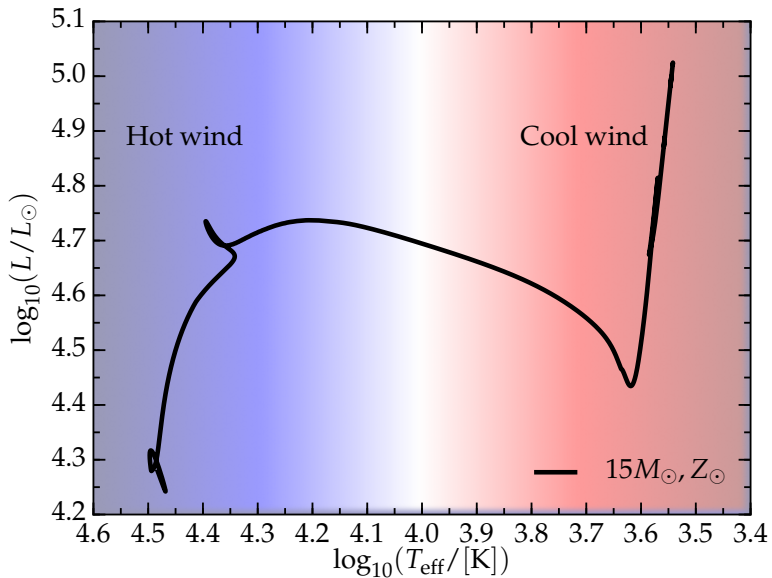
Bruch *et al.* 2023, see also, e.g., Kochanek 2012, Khazov *et al.* 2016



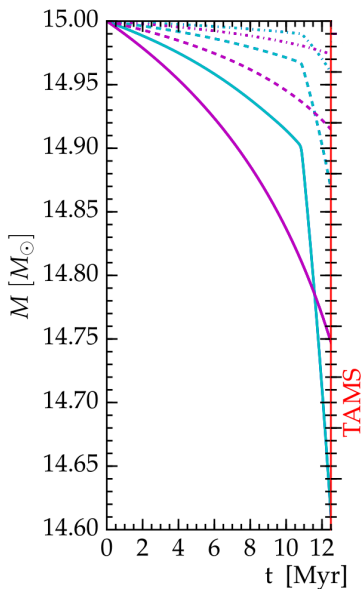
modified from Jacobson-Galan *et al.* 2023

Single star wind uncertainties

Combination of algorithms



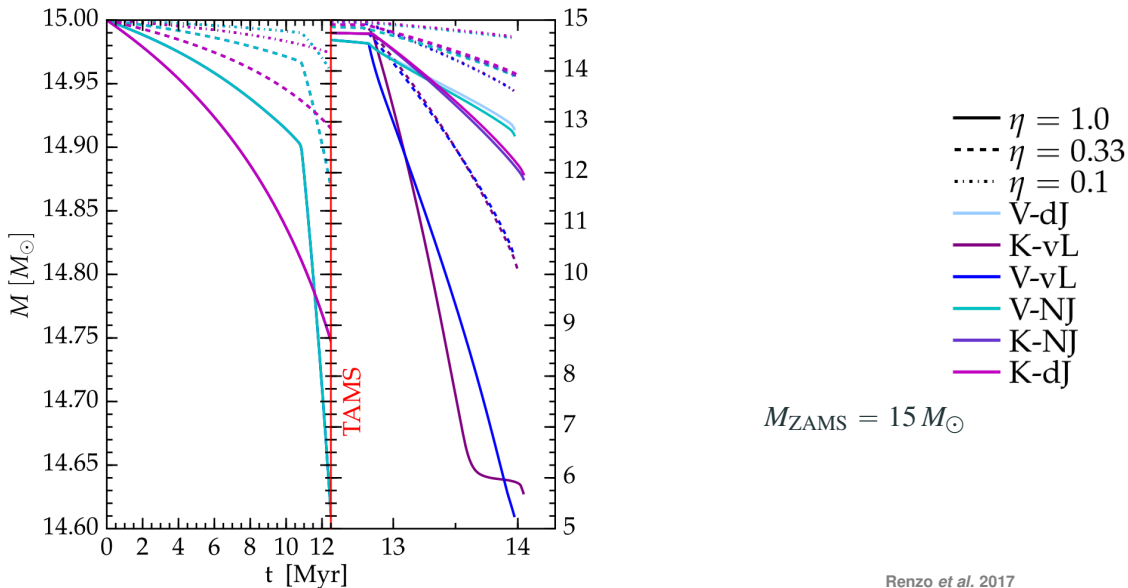
Wind mass loss history



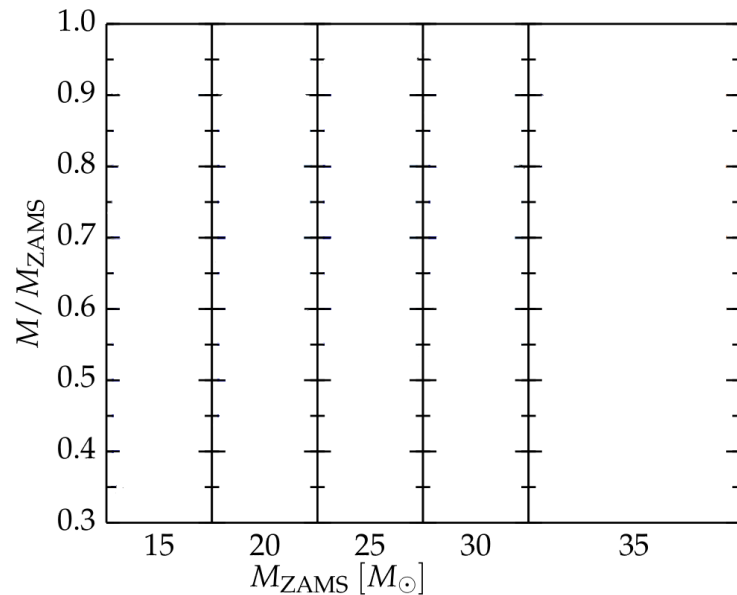
- $\eta = 1.0$
- - - $\eta = 0.33$
- ⋯ $\eta = 0.1$
- V-dJ
- K-vL
- V-vL
- V-NJ
- K-NJ
- K-dJ

$$M_{\text{ZAMS}} = 15 M_{\odot}$$

Wind mass loss history



Impact on the final mass

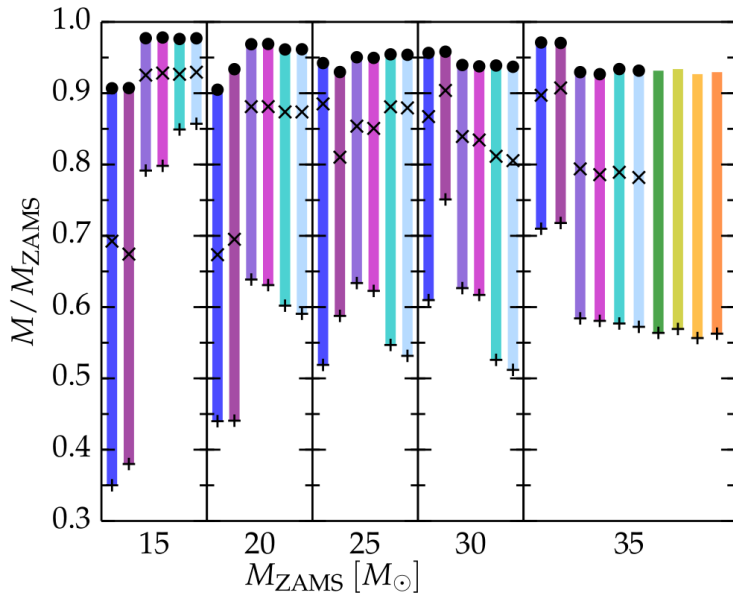


MESA

Legend:

- $\eta = 0.1$
- ✕ $\eta = 0.33$
- + $\eta = 1.0$

Impact on the final mass



MESA

Legend:

- $\eta = 0.1$
- ✕ $\eta = 0.33$
- + $\eta = 1.0$