

$$H_{l-doubling}=2\pi\hbar c\sum_t\sum_{\pm}\frac{B_e^2}{\omega_s}\Bigg[q_{t\pm}^2+2\Bigg(q_{t\pm}^2+\frac{p_{t\pm}^2}{\hbar^2}\Bigg)\sum_s\frac{\big(\zeta_{ts}^x\big)^2\omega_2^2}{\omega_t^2-\omega_2^2}\Bigg]J_{\pm}^2+\frac{q_{tD}}{2}\left\{H_{t:l-doubling},(J-S)^2\right\}$$